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Behdad et al.

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(54) **2-BIT PHASE QUANTIZATION PHASED ARRAY ELEMENT**

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(57) **ABSTRACT**

(51) **Int. Cl.**
H01Q 3/38 (2006.01)
H01Q 15/00 (2006.01)
H01Q 3/24 (2006.01)

A phase shift element includes a first dielectric layer, a conductive layer, a second dielectric layer, a conducting pattern layer, switches, and vertical interconnect accesses (vias). Each conductor of a plurality of conductors of the conducting pattern layer is orthogonal to two other conductors. Each switch is switchable between a conducting position and a non-conducting position. Each via is connected to a single conductor. The first conductive material reflects an electromagnetic wave incident on the conducting pattern layer and on the second dielectric layer. When a switch is in the conducting position, the switch electrically connects two conductors to each other through their respective vias. A plurality of different switch configurations of the switches provide a 2-bit phase quantization on the reflected electromagnetic wave relative to the electromagnetic wave incident on the conducting pattern layer when the electromagnetic wave is incident on the conducting pattern layer.

(52) **U.S. Cl.**
CPC **H01Q 3/38** (2013.01); **H01Q 3/247** (2013.01); **H01Q 15/002** (2013.01)

(58) **Field of Classification Search**
CPC H01Q 9/04; H01Q 15/14; H01Q 19/06; H01Q 19/17; H01Q 3/38; H01Q 3/247;
(Continued)

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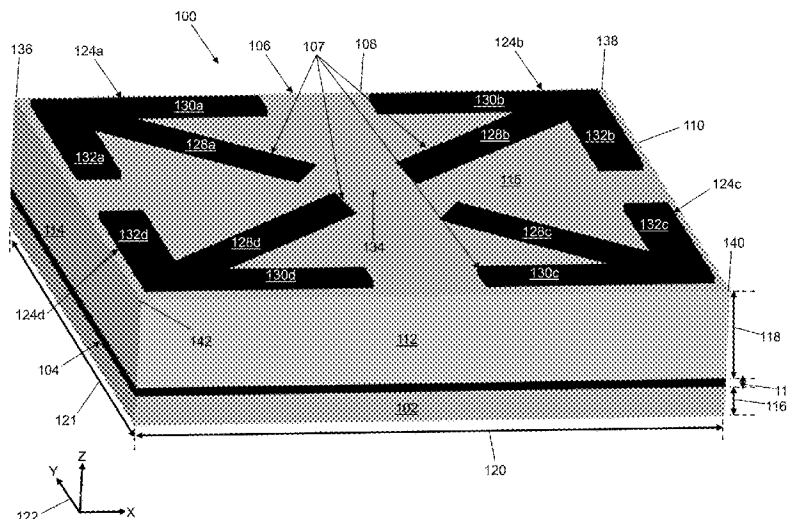
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20 Claims, 31 Drawing Sheets



(58) **Field of Classification Search**

CPC .. H01Q 15/002; H01Q 15/148; H01Q 15/006;
H01Q 15/0006; H01Q 1/42; H01Q 15/24
See application file for complete search history.

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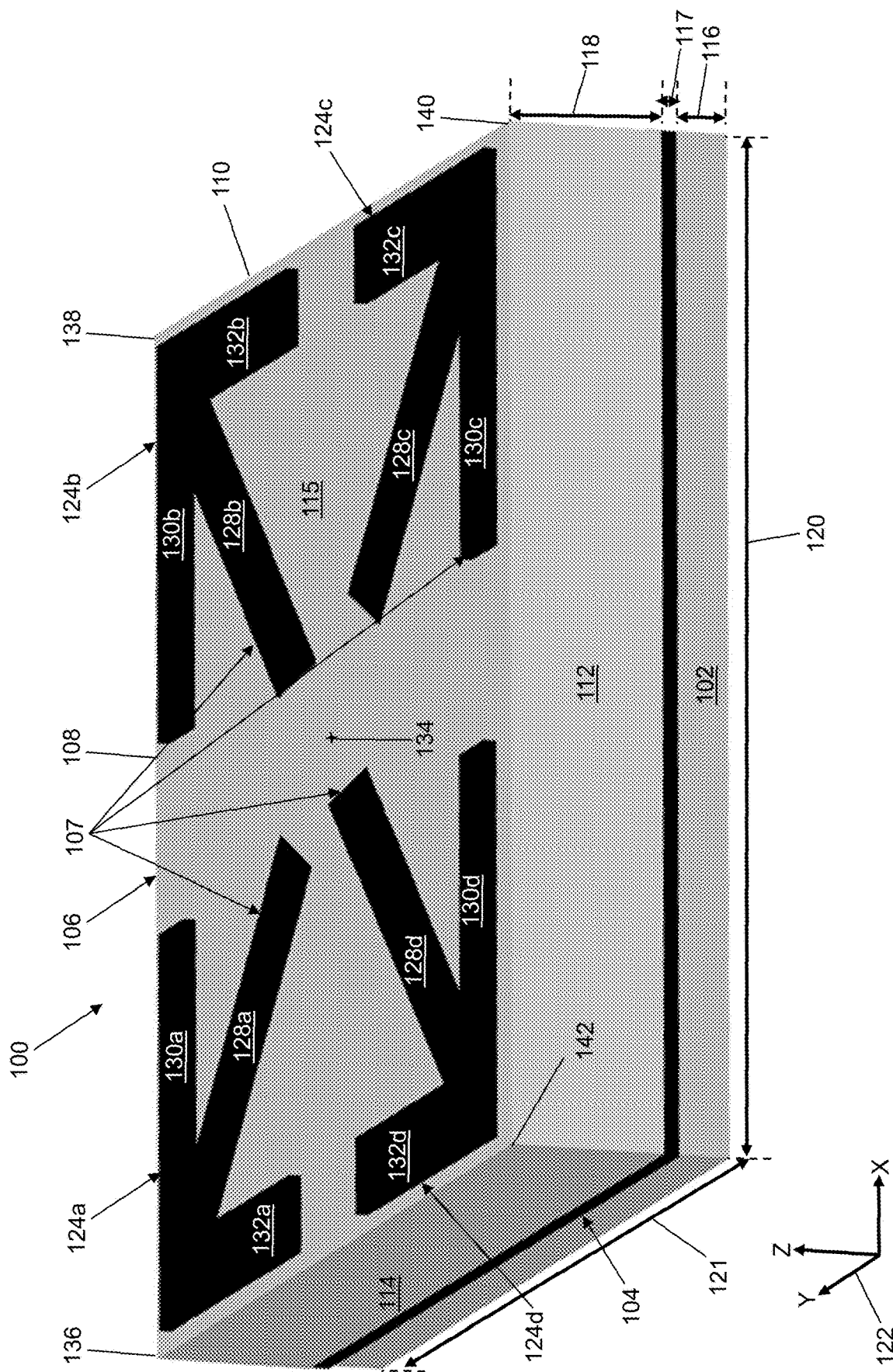
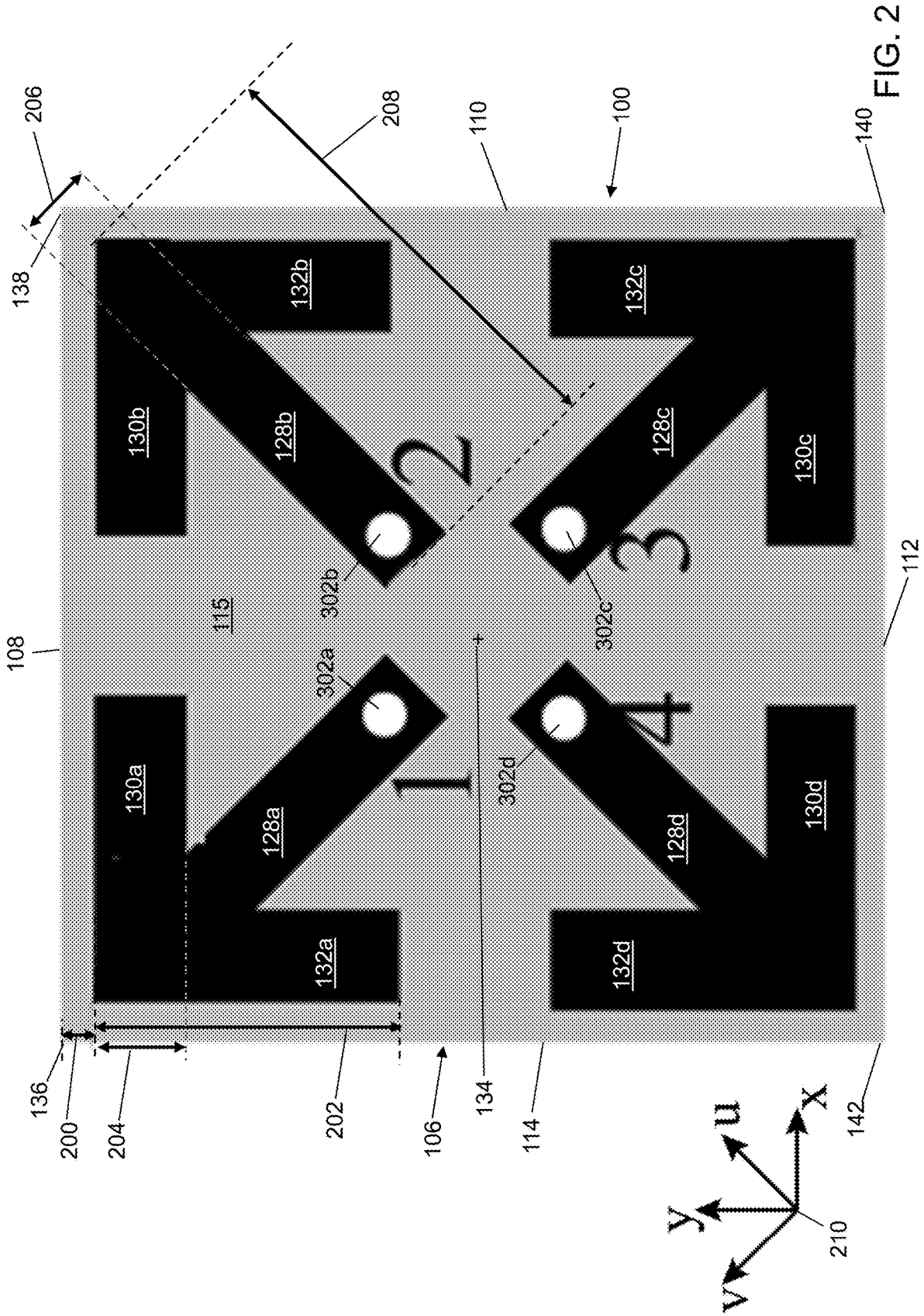


FIG. 1



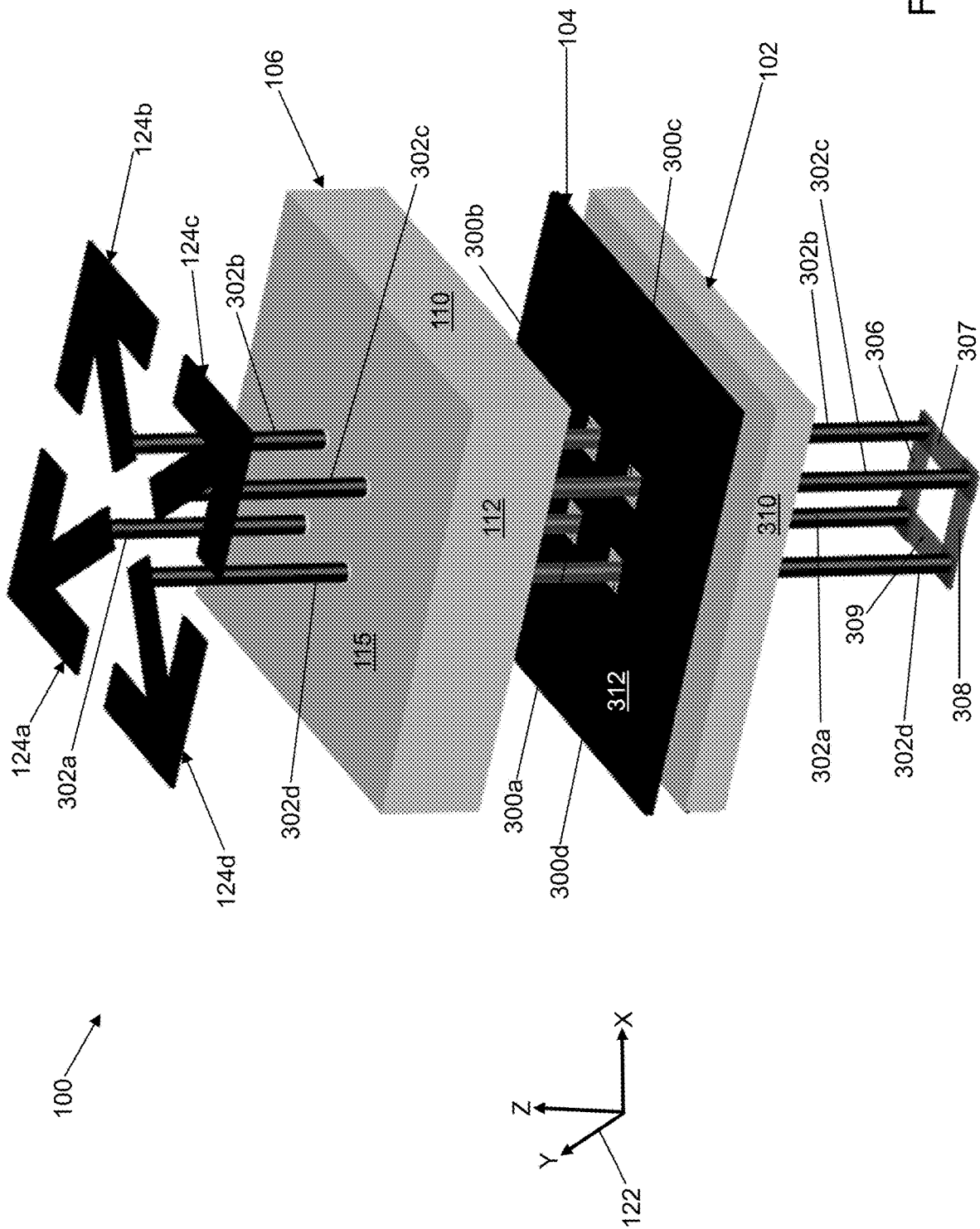


FIG. 3

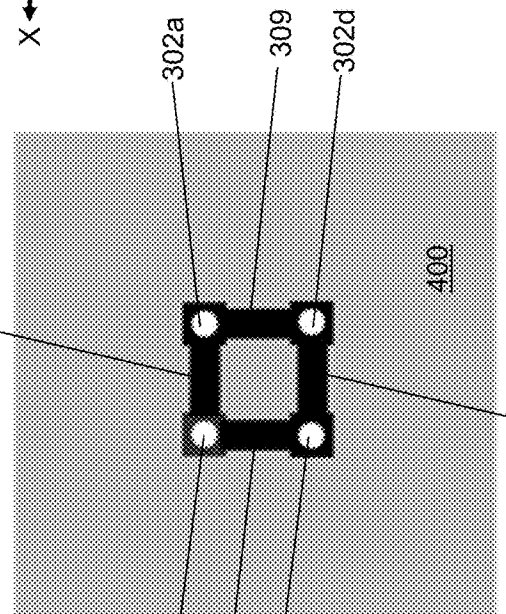
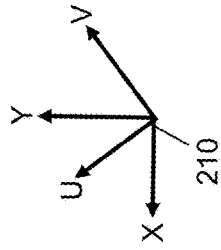
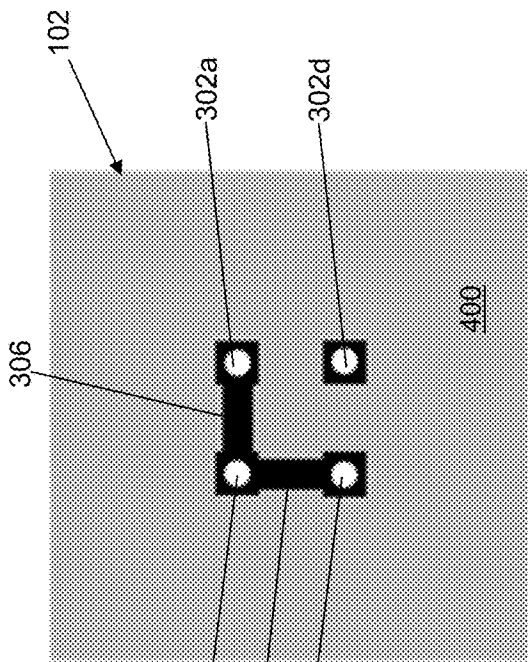
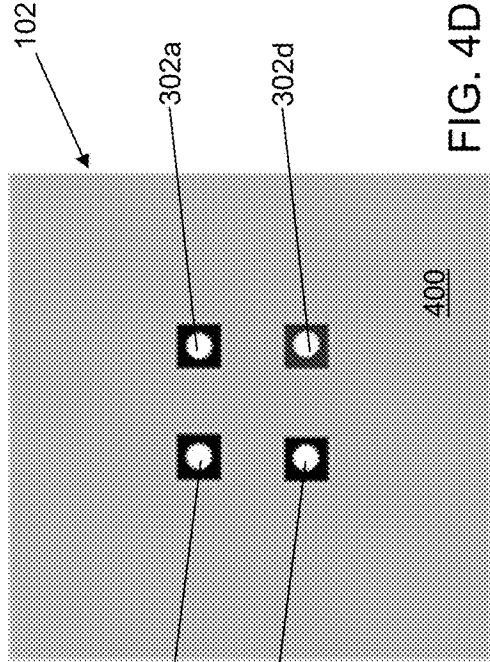
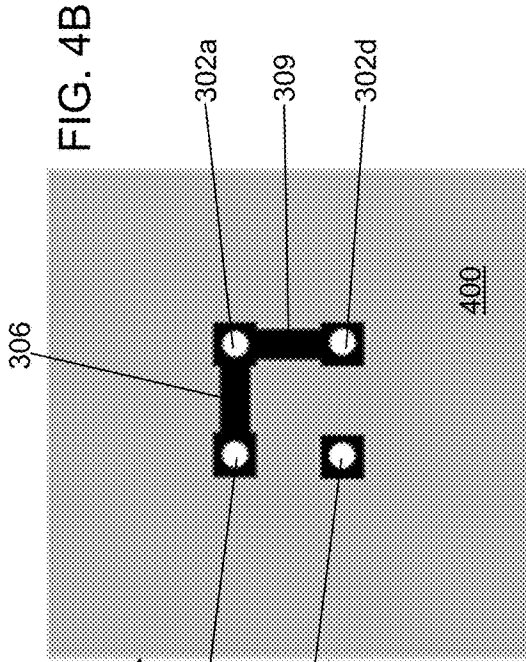


FIG. 4A

FIG. 4C

FIG. 4B

FIG. 4D

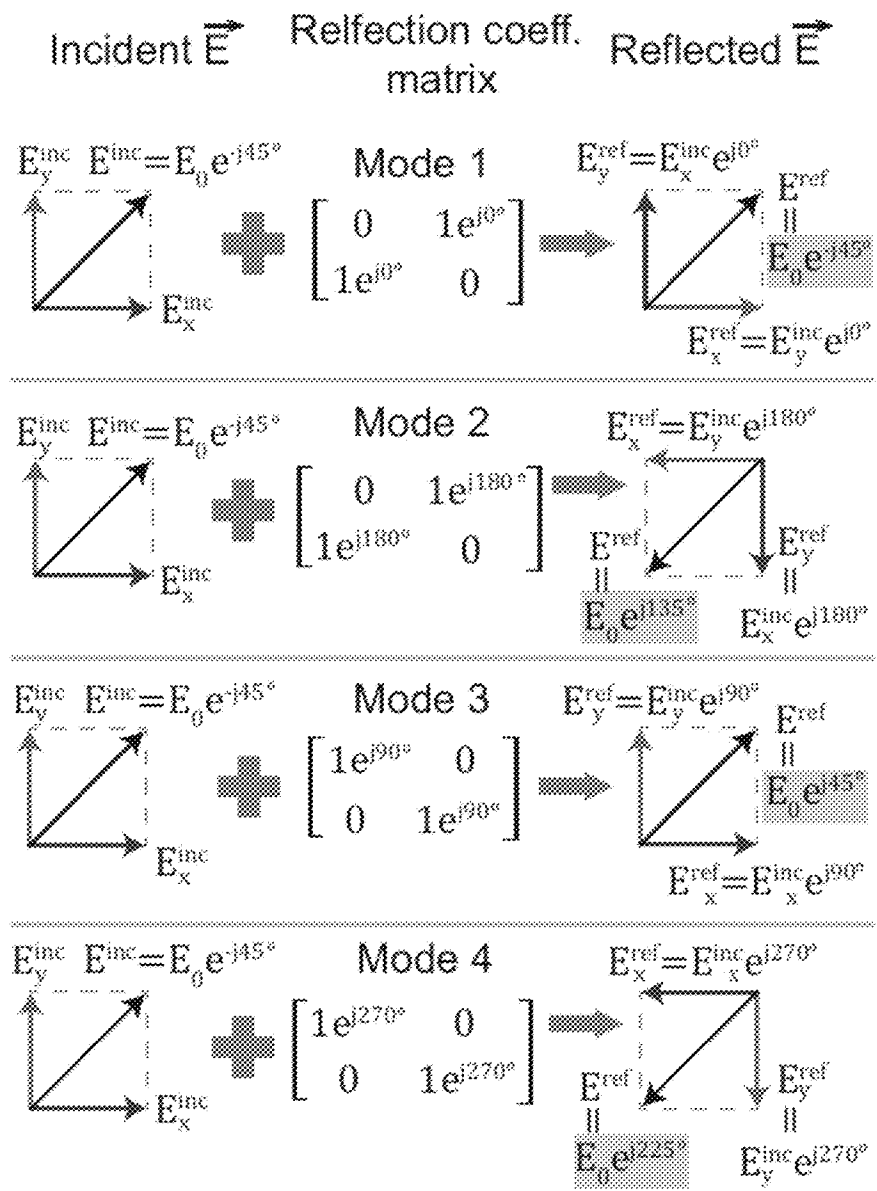


FIG. 4E

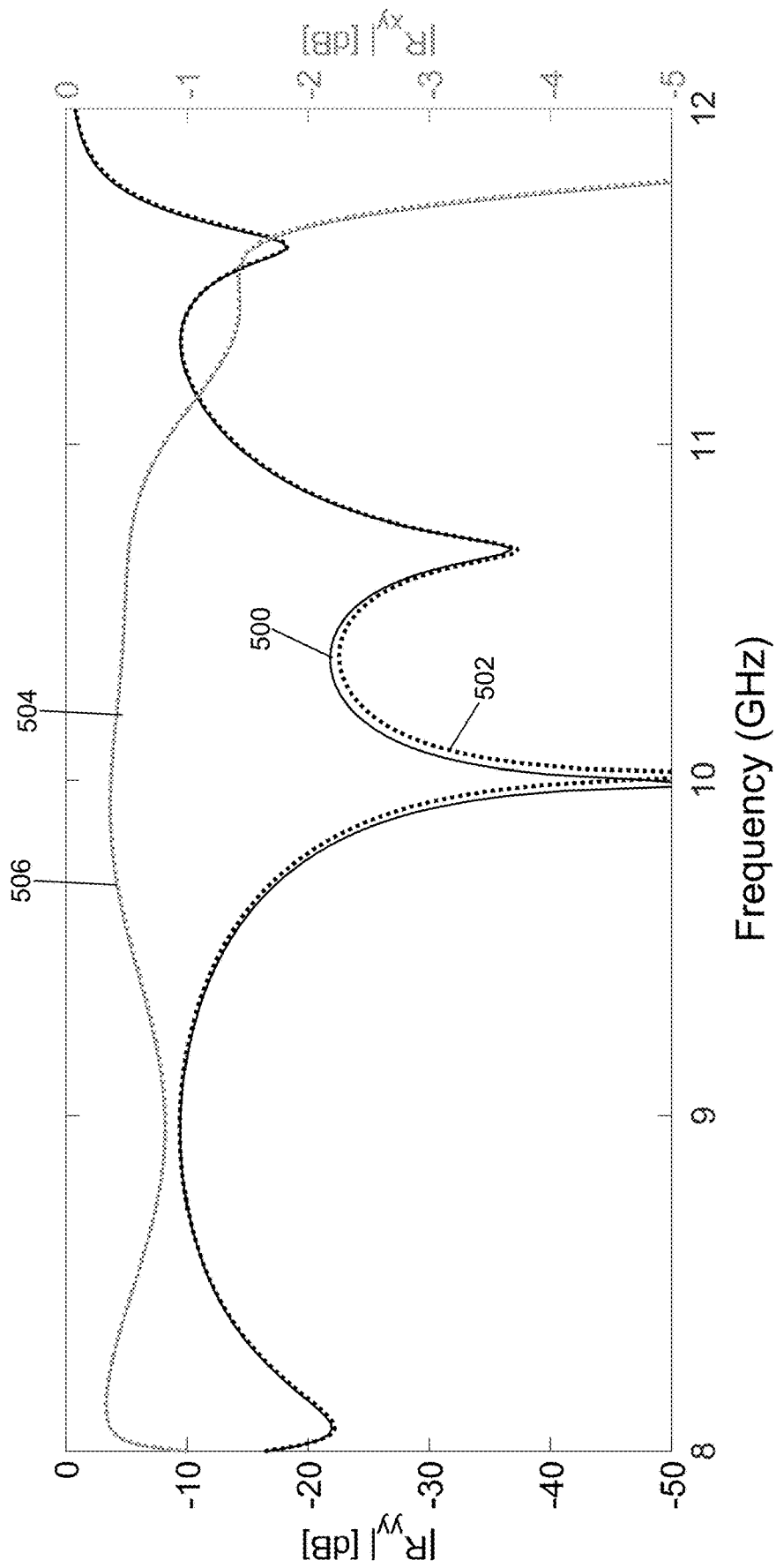


FIG. 5A

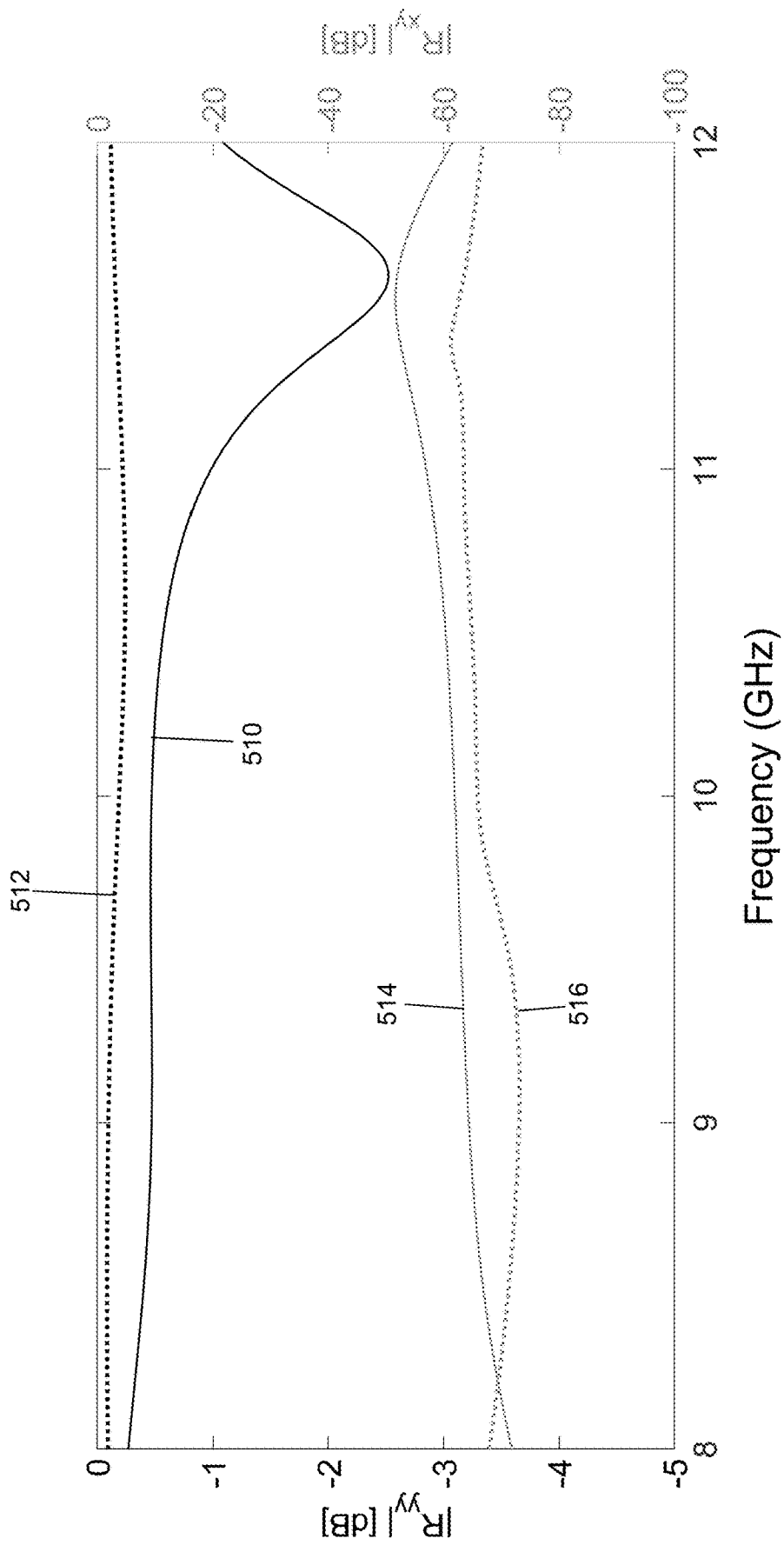


FIG. 5B

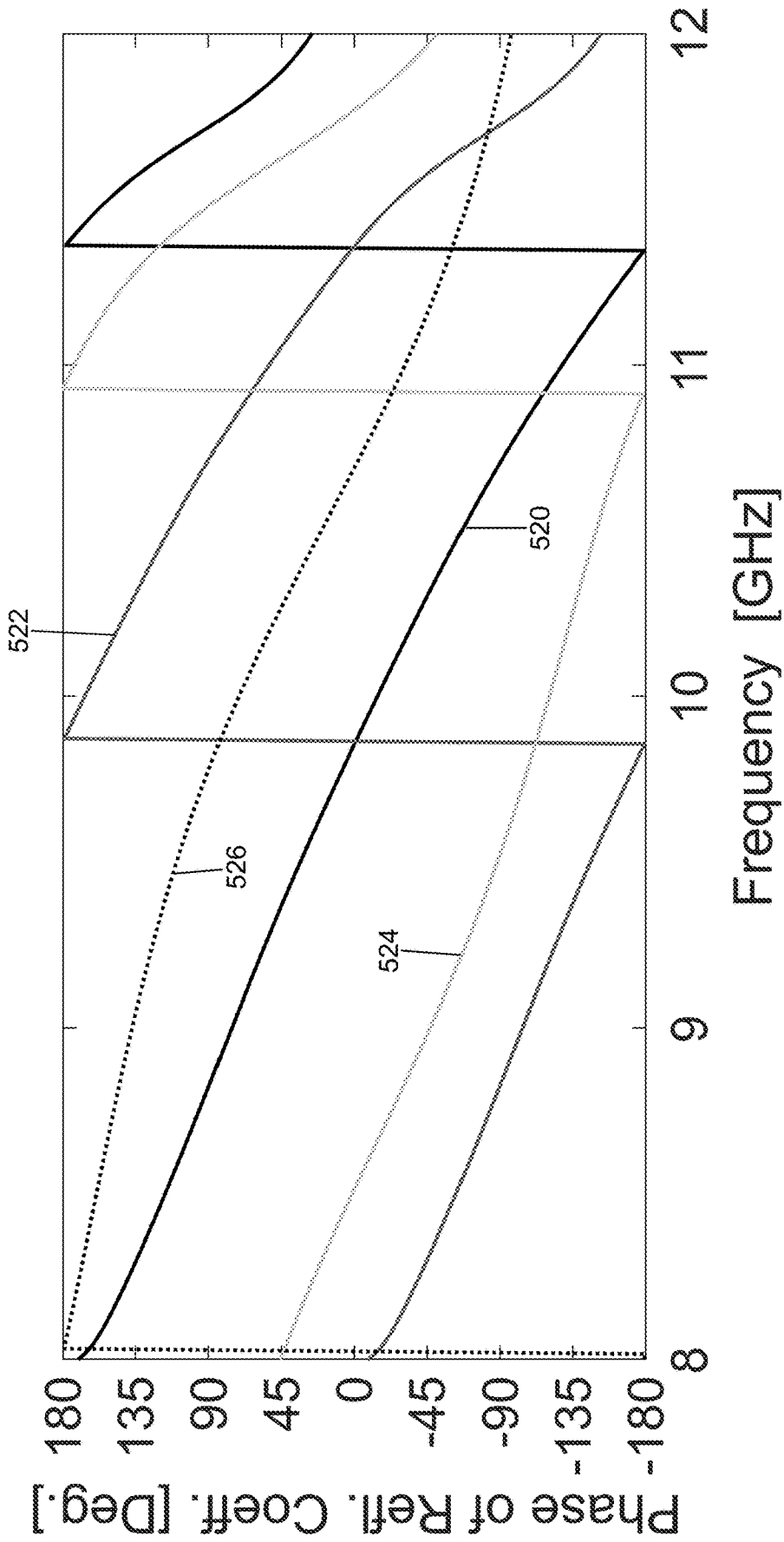


FIG. 5C

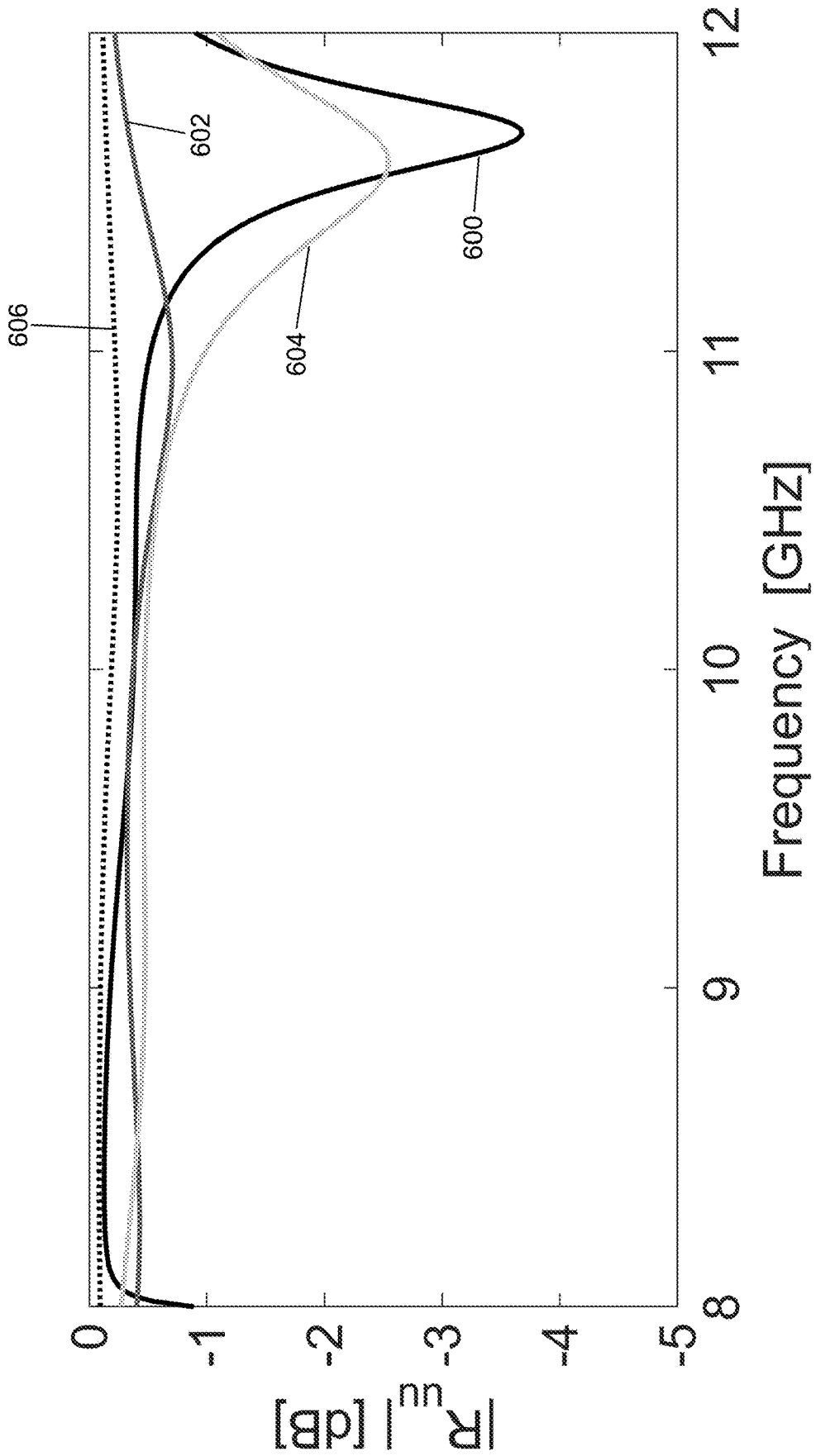


FIG. 6A

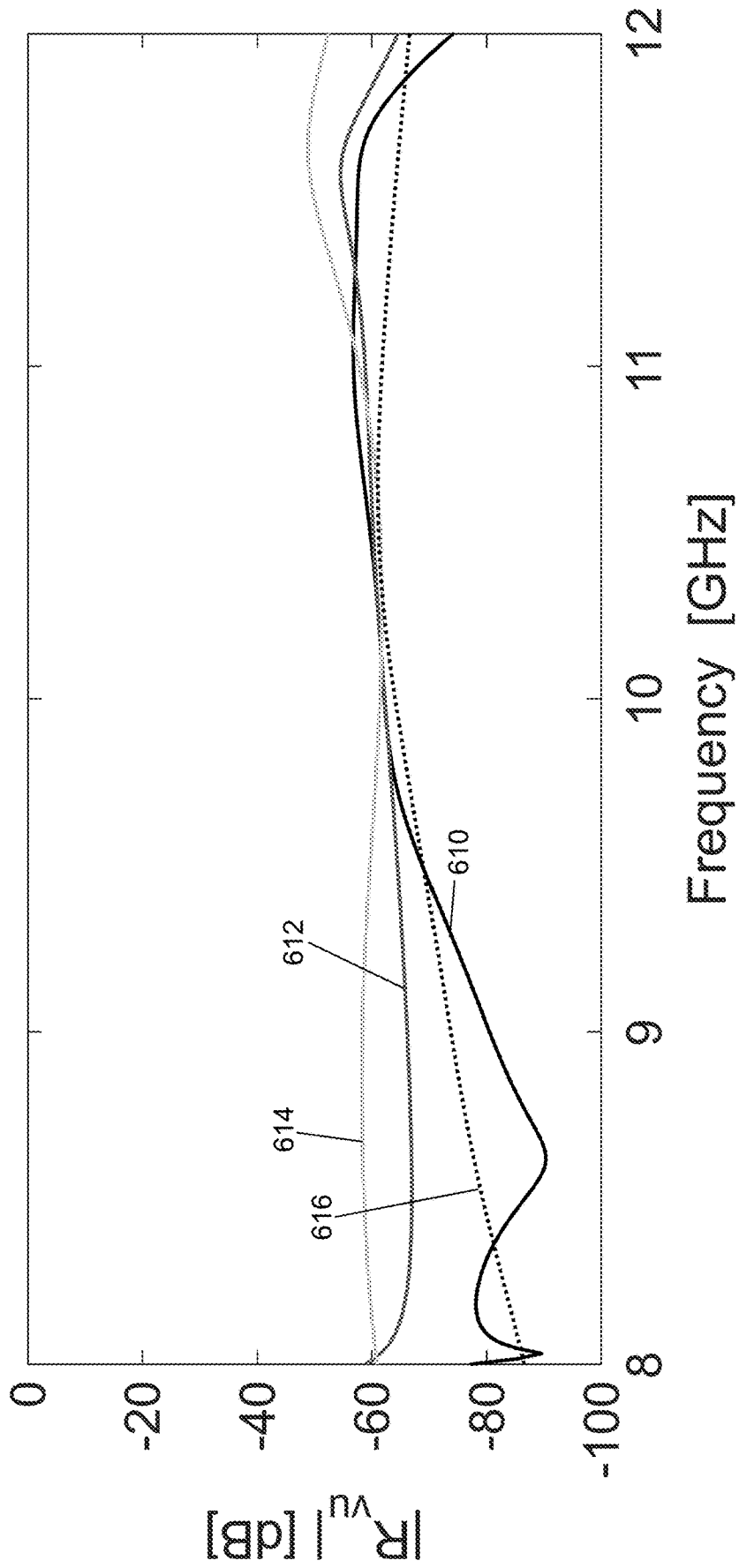


FIG. 6B

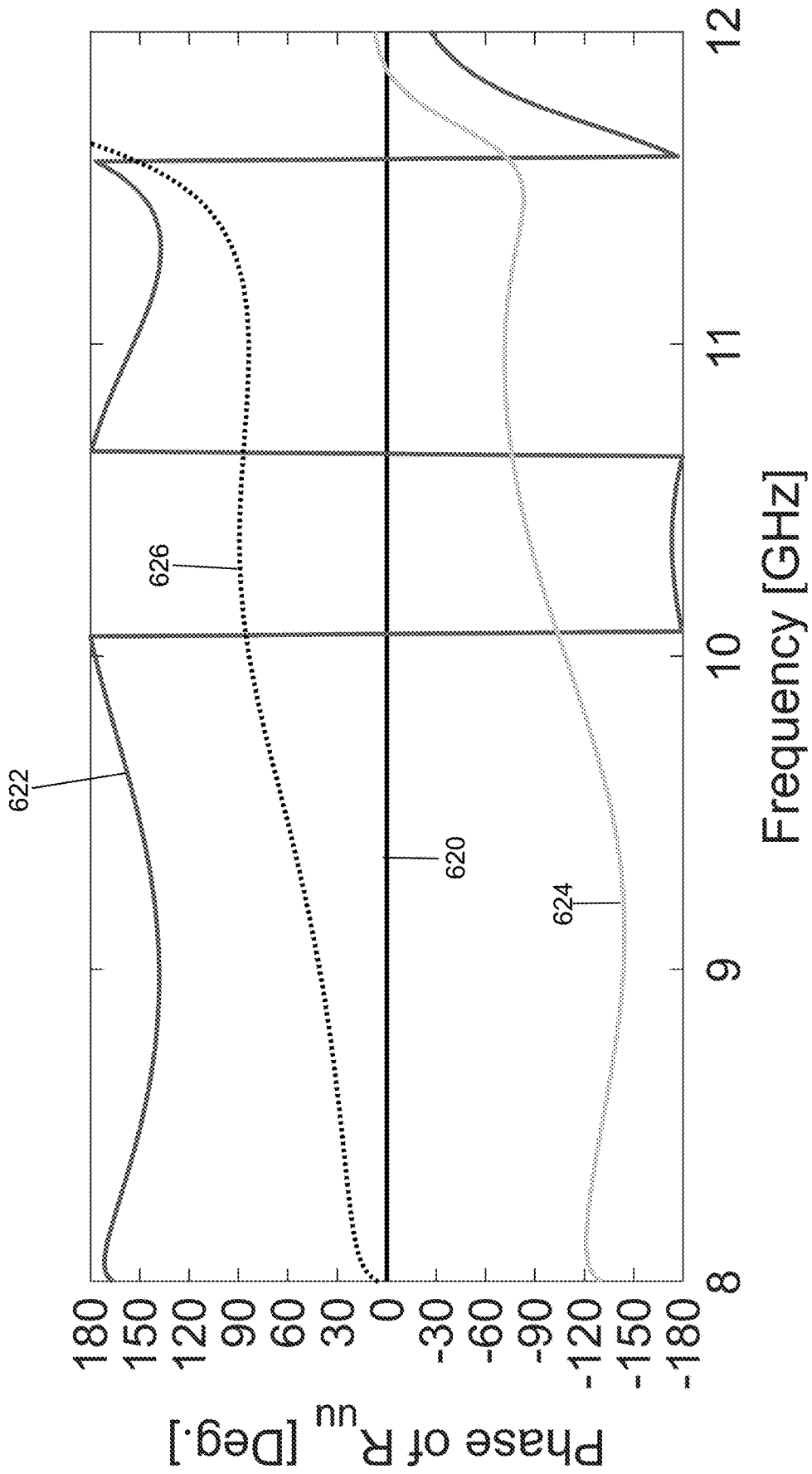


FIG. 6C

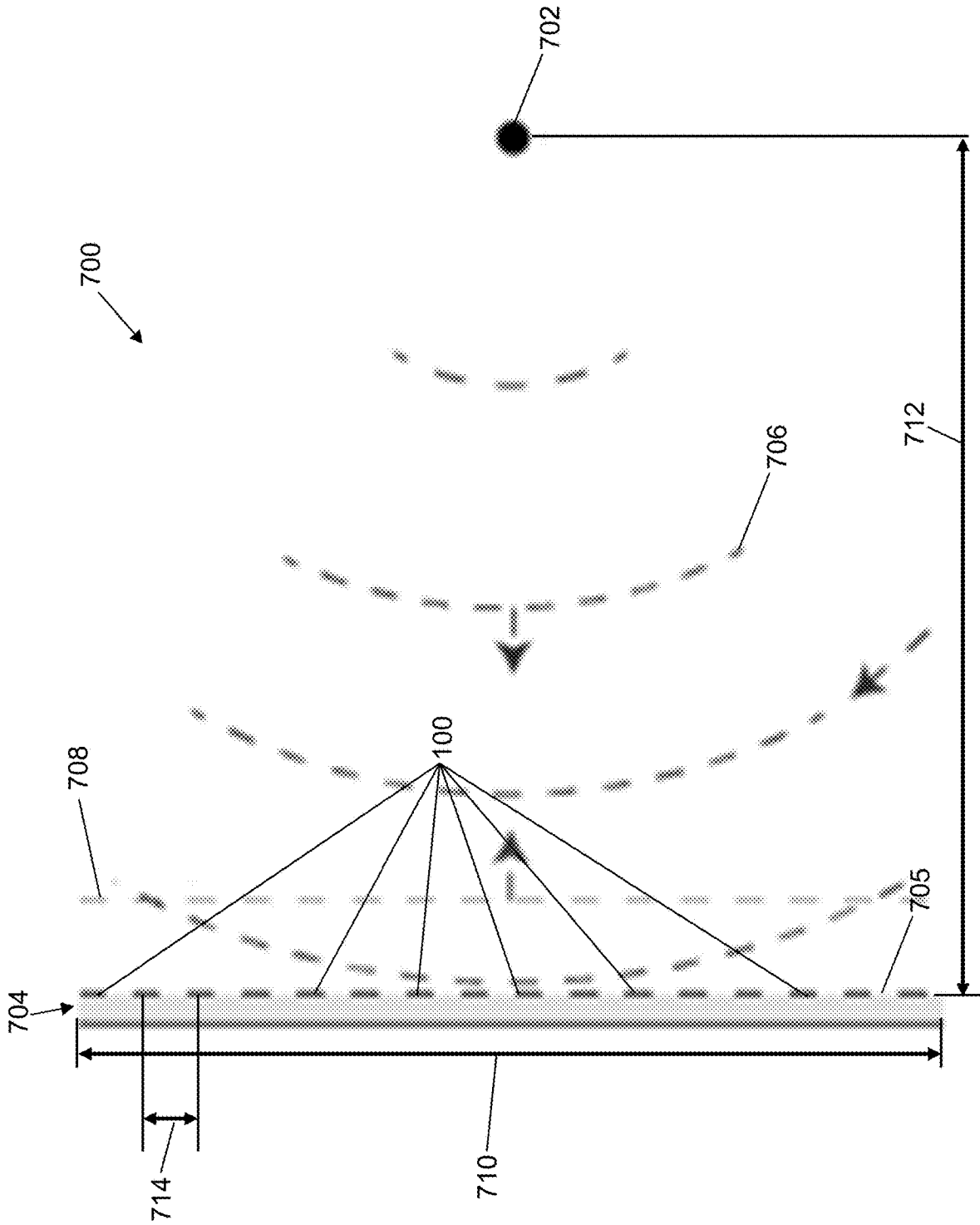


FIG. 7

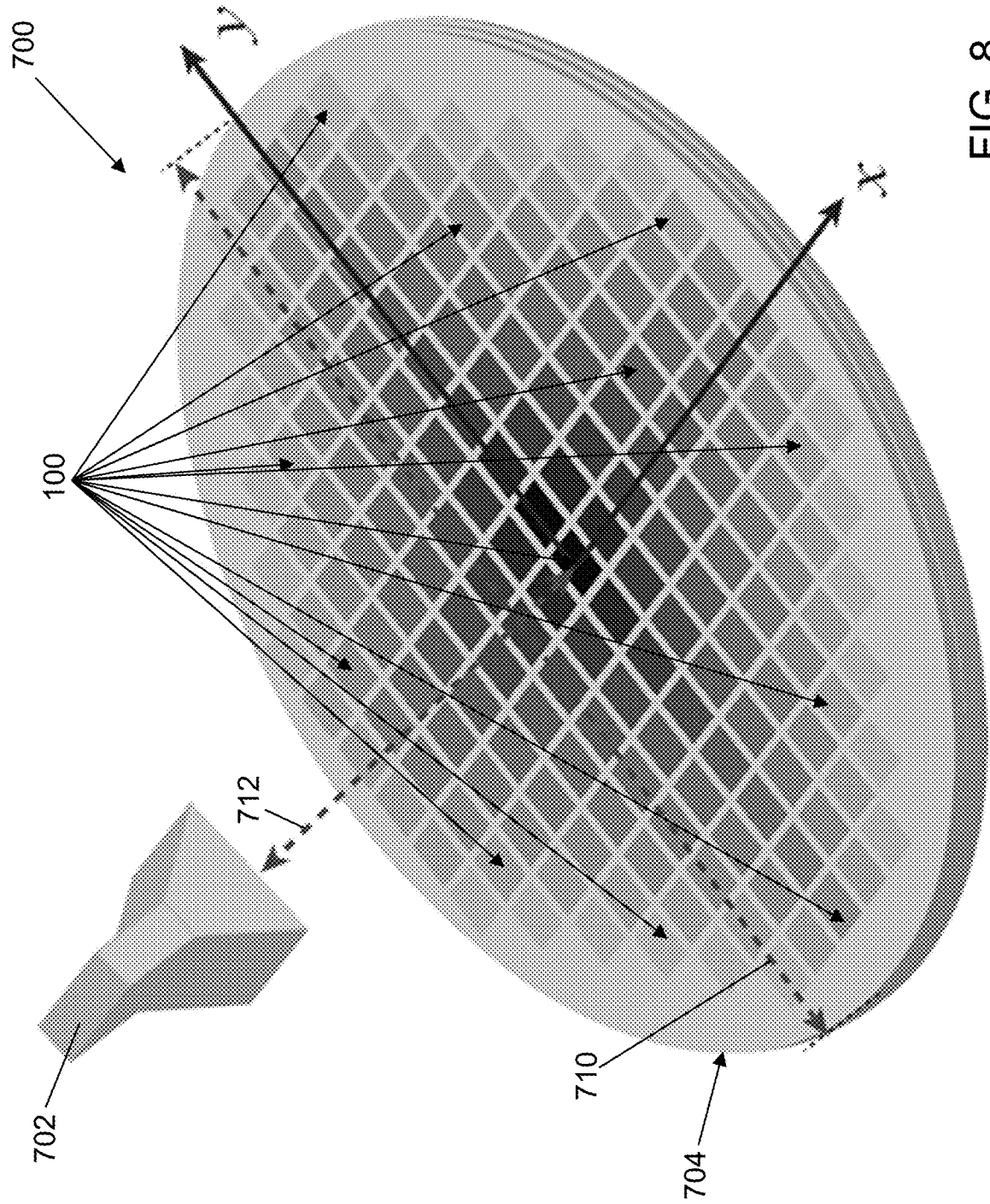


FIG. 8

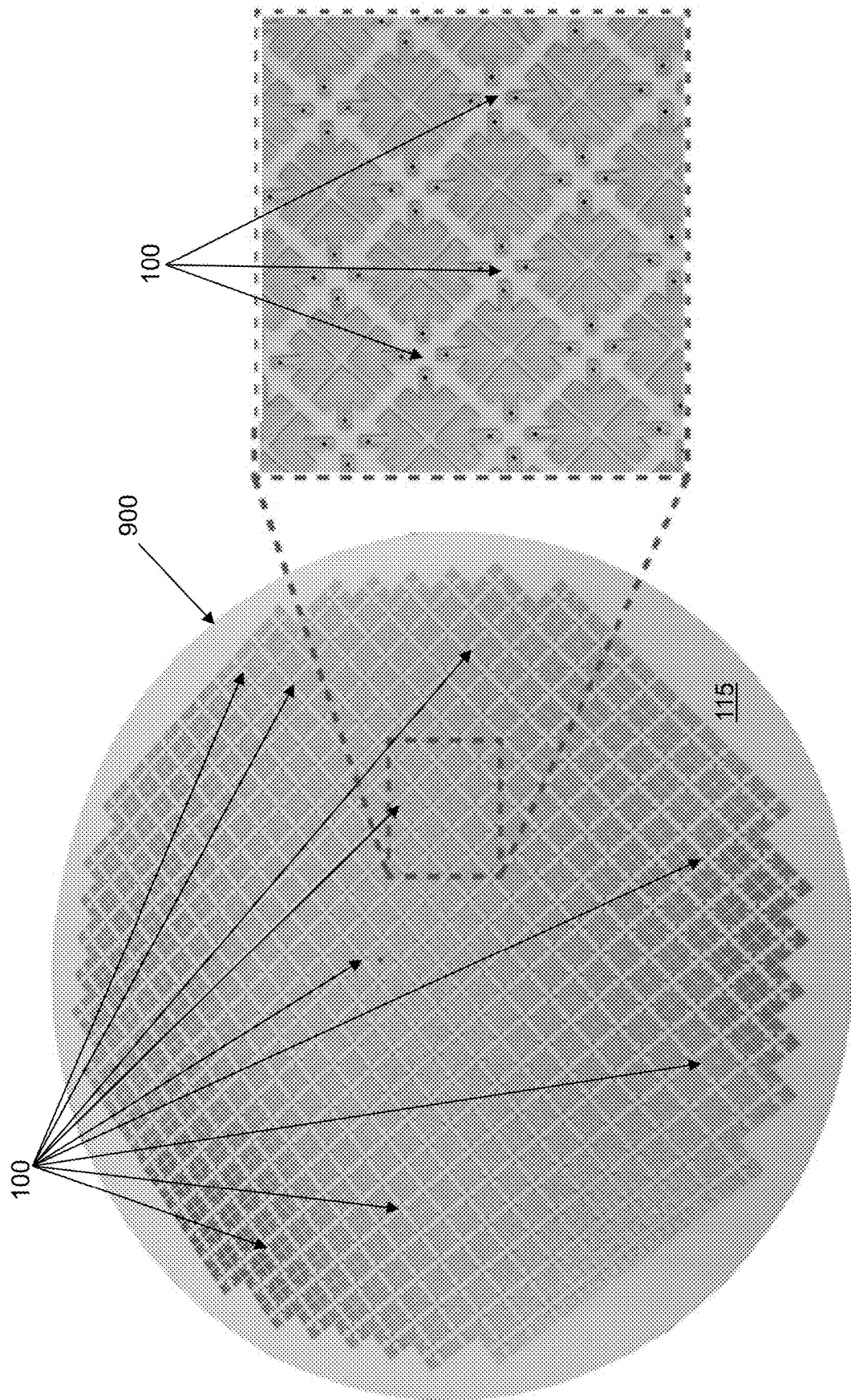


FIG. 9A

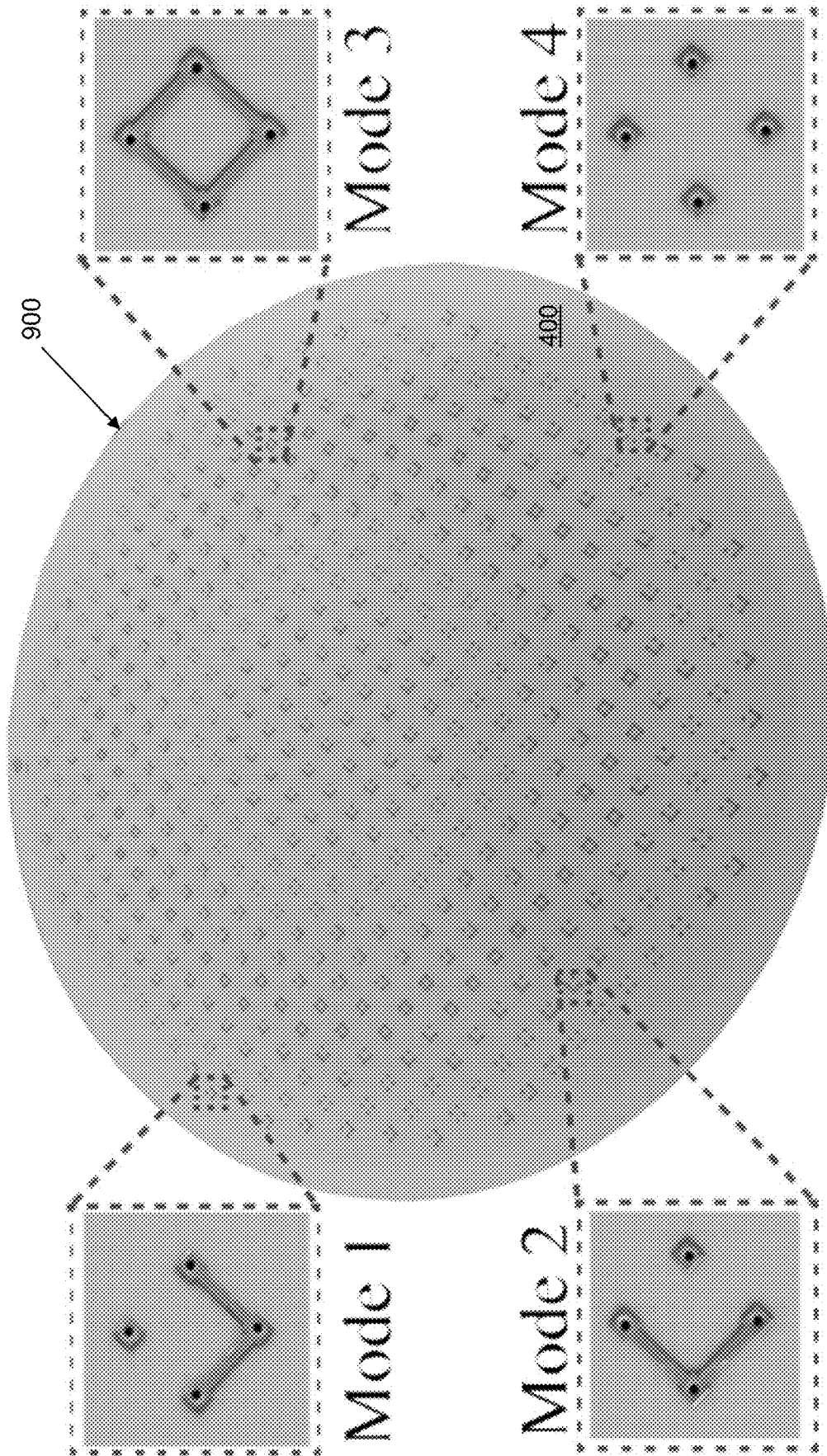


FIG. 9B

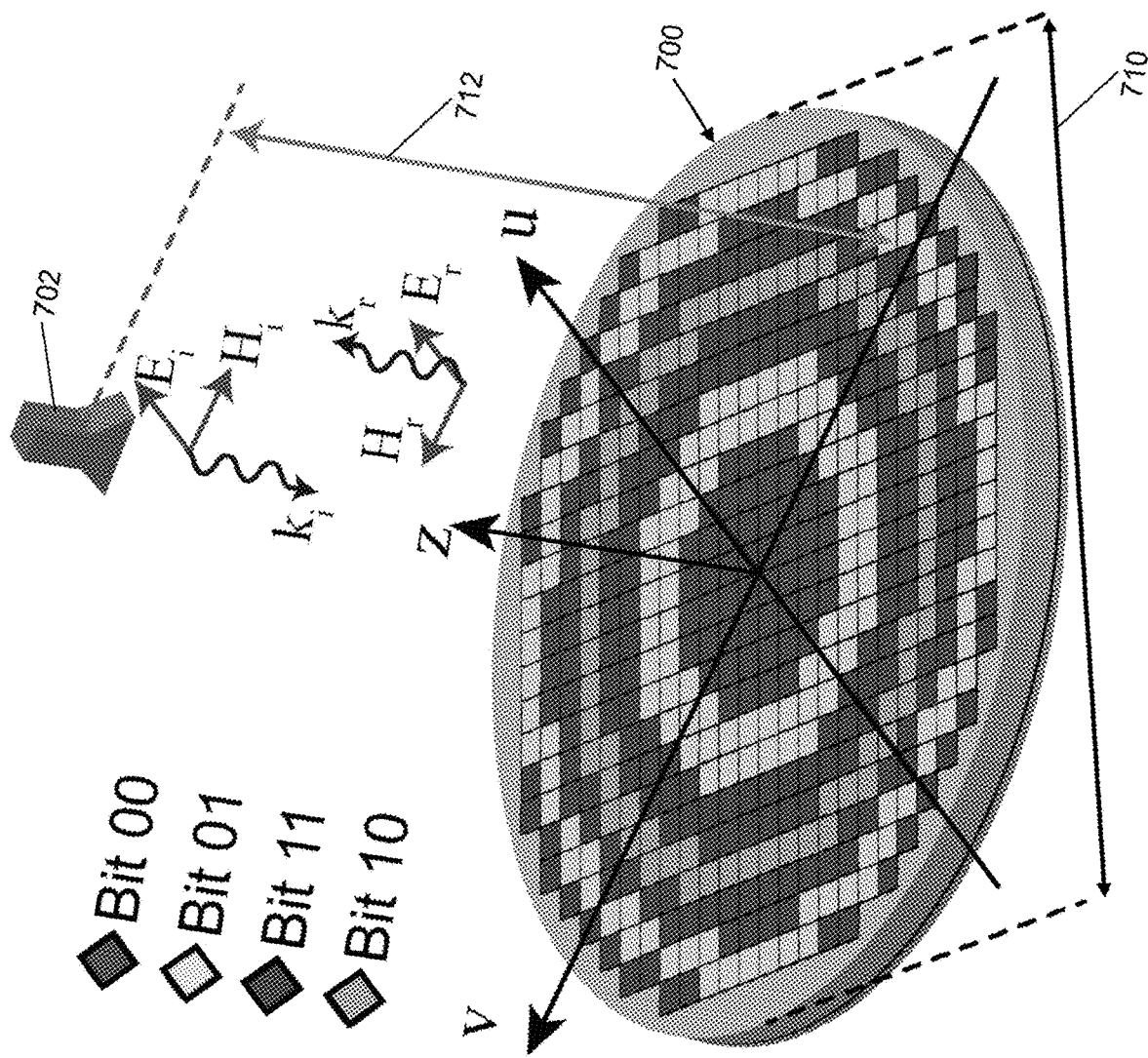


FIG. 10

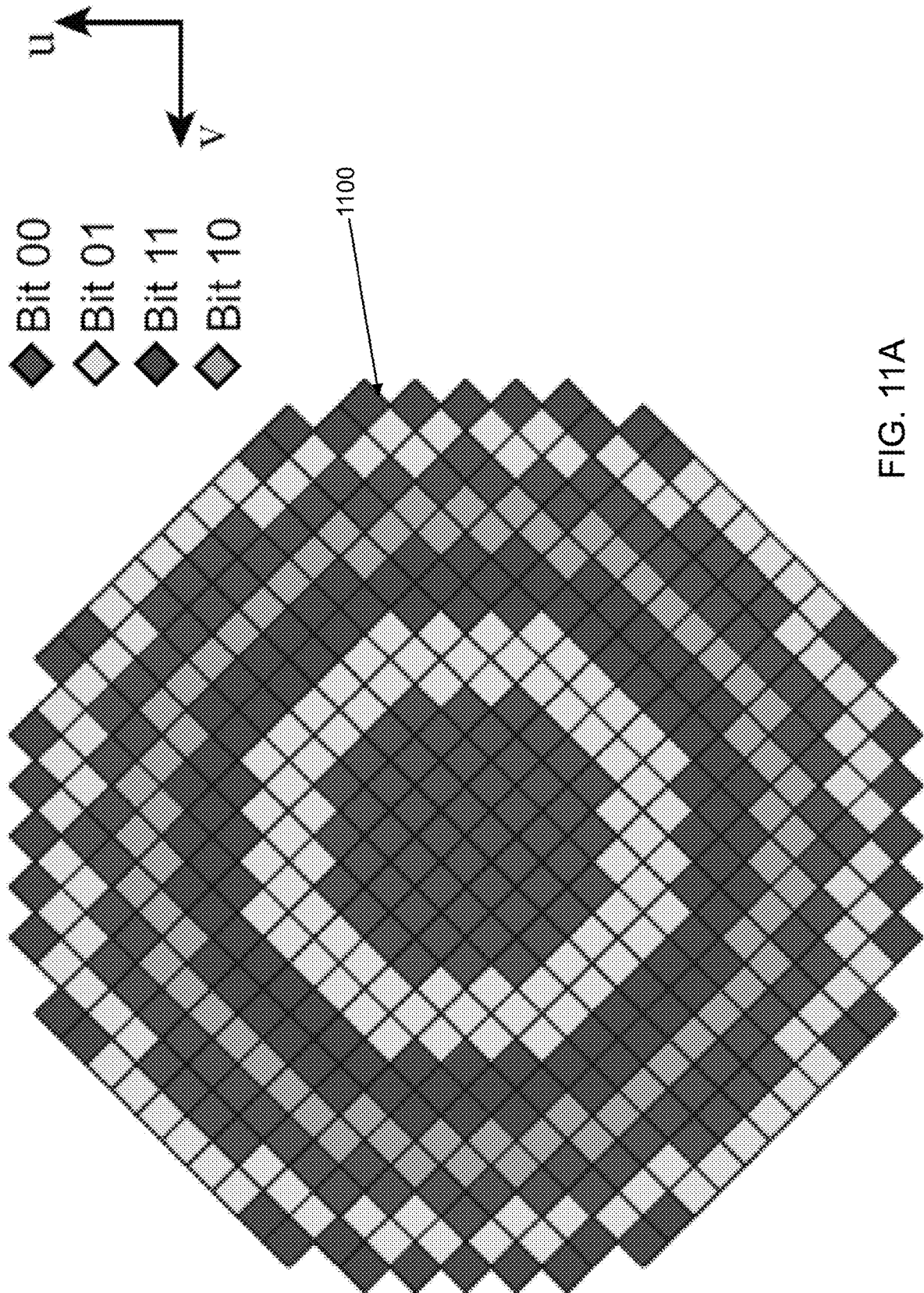


FIG. 11A

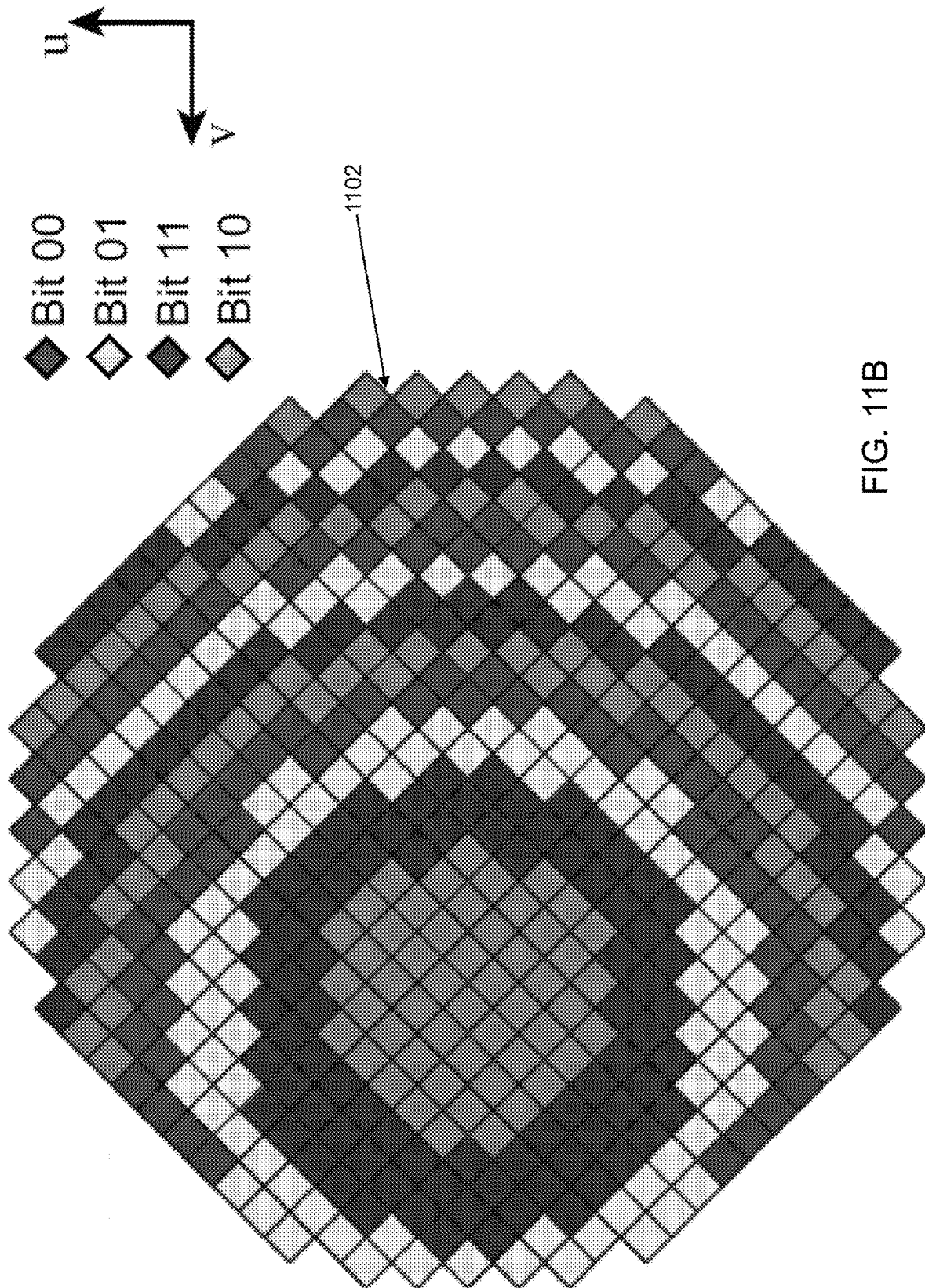


FIG. 11B

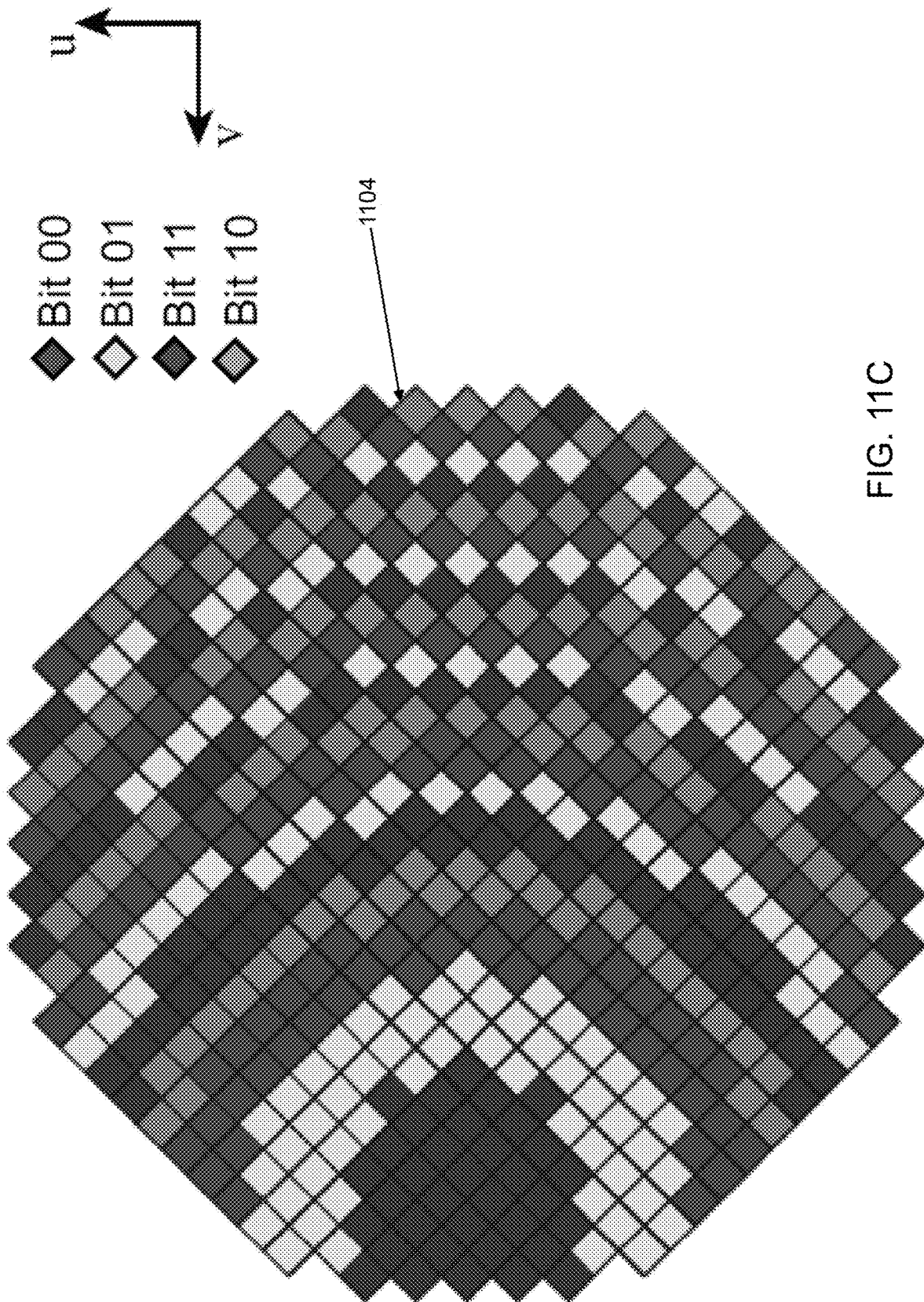


FIG. 11C

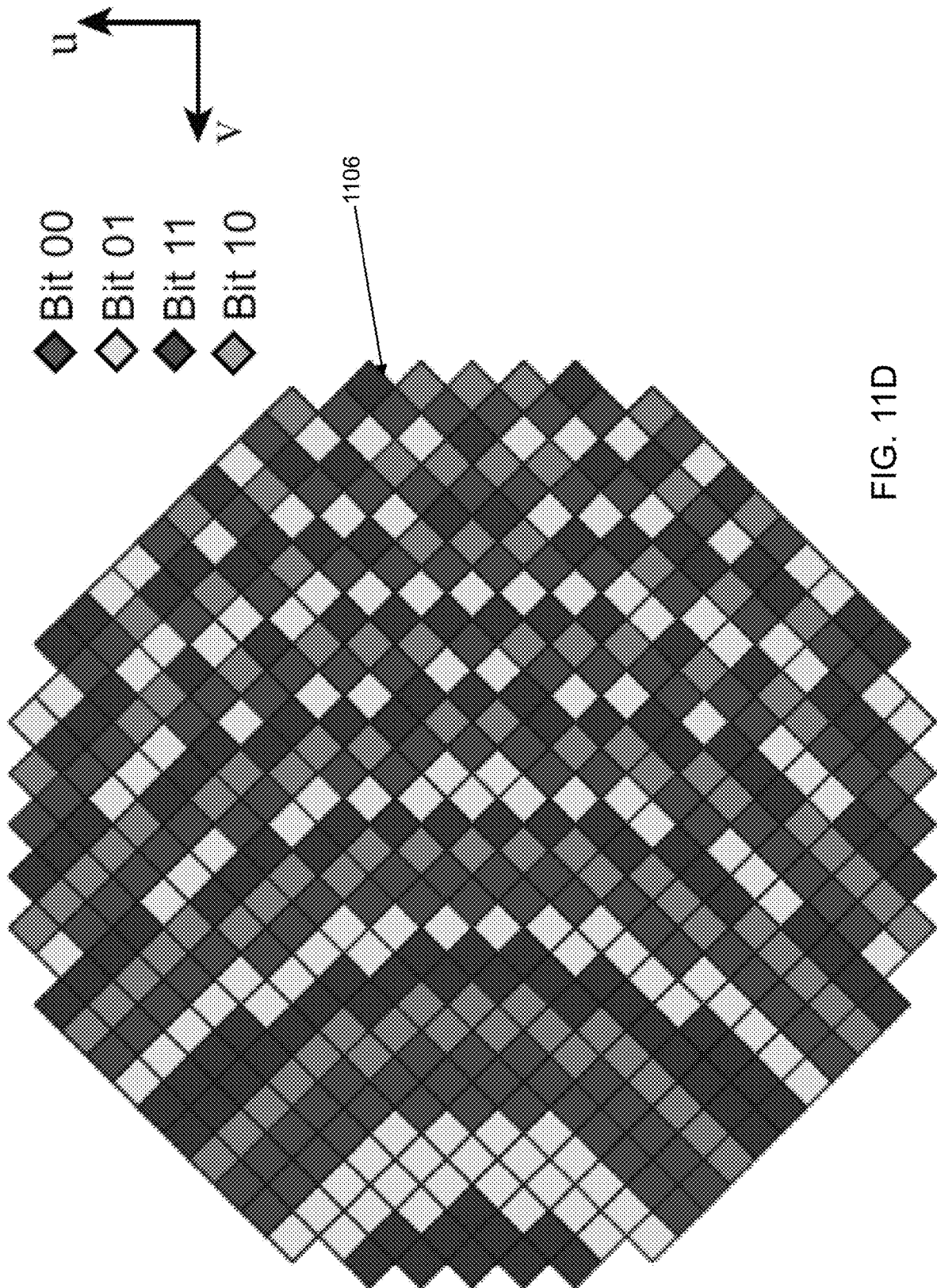


FIG. 11D

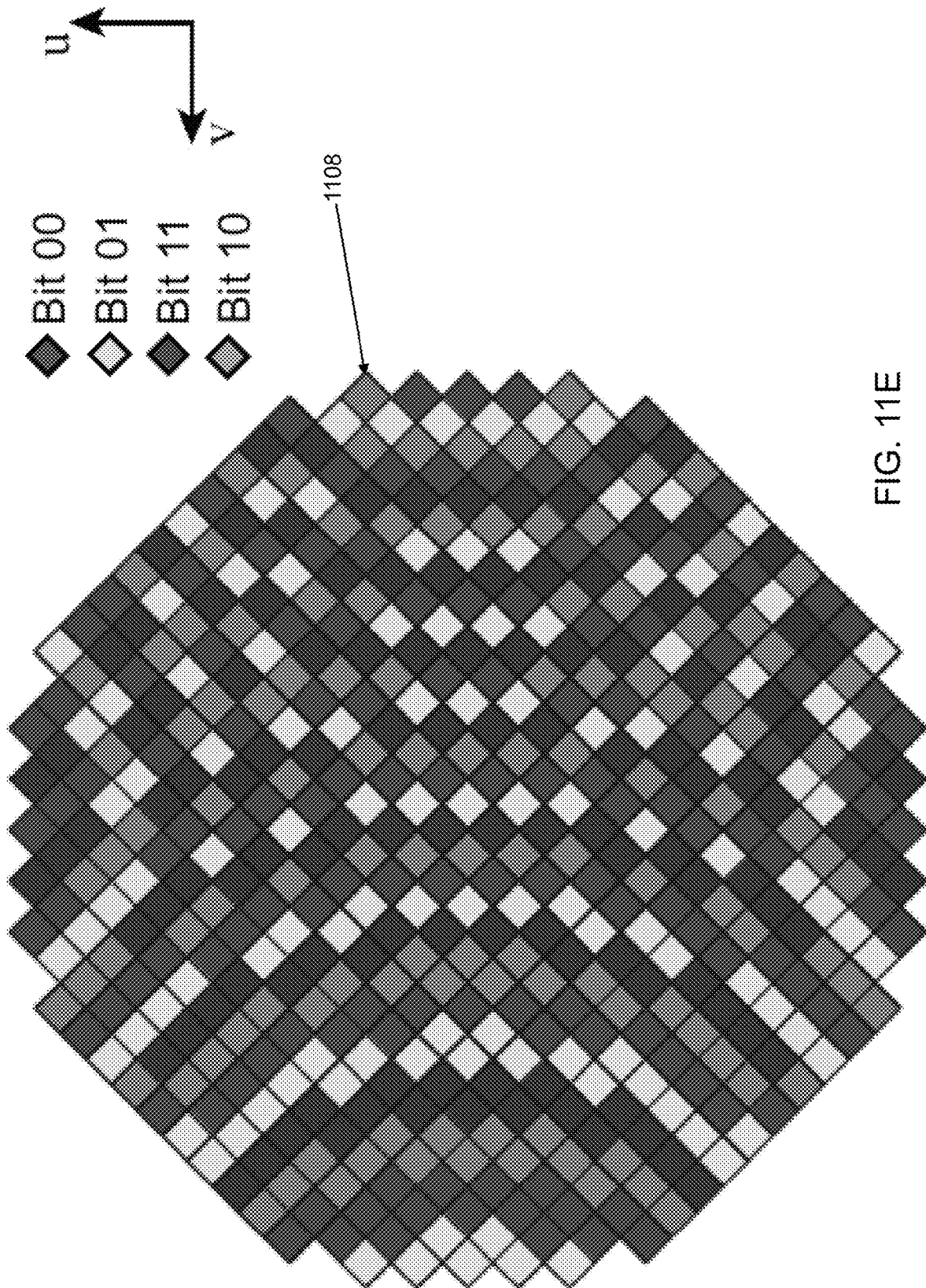


FIG. 11E

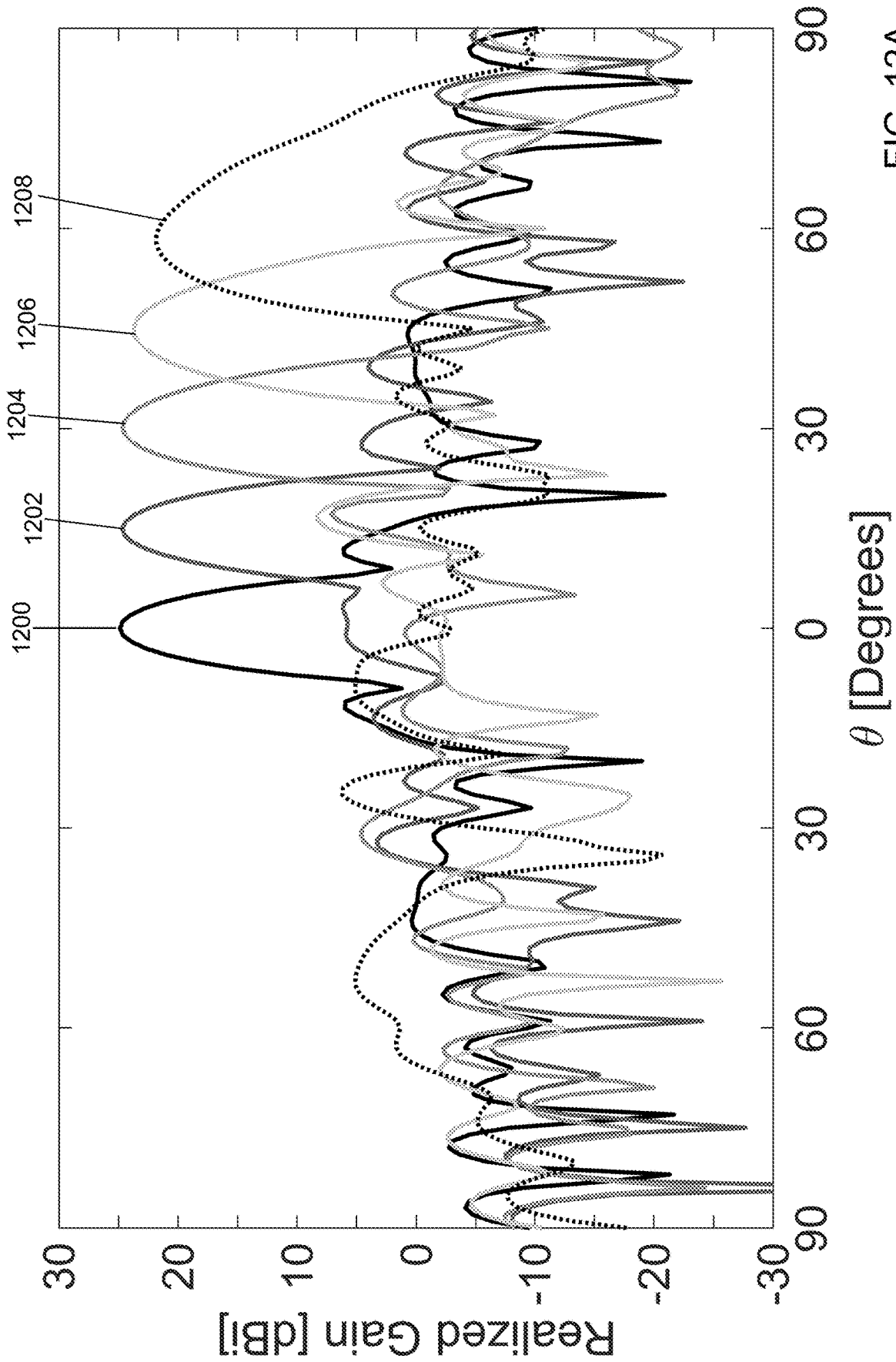


FIG. 12A

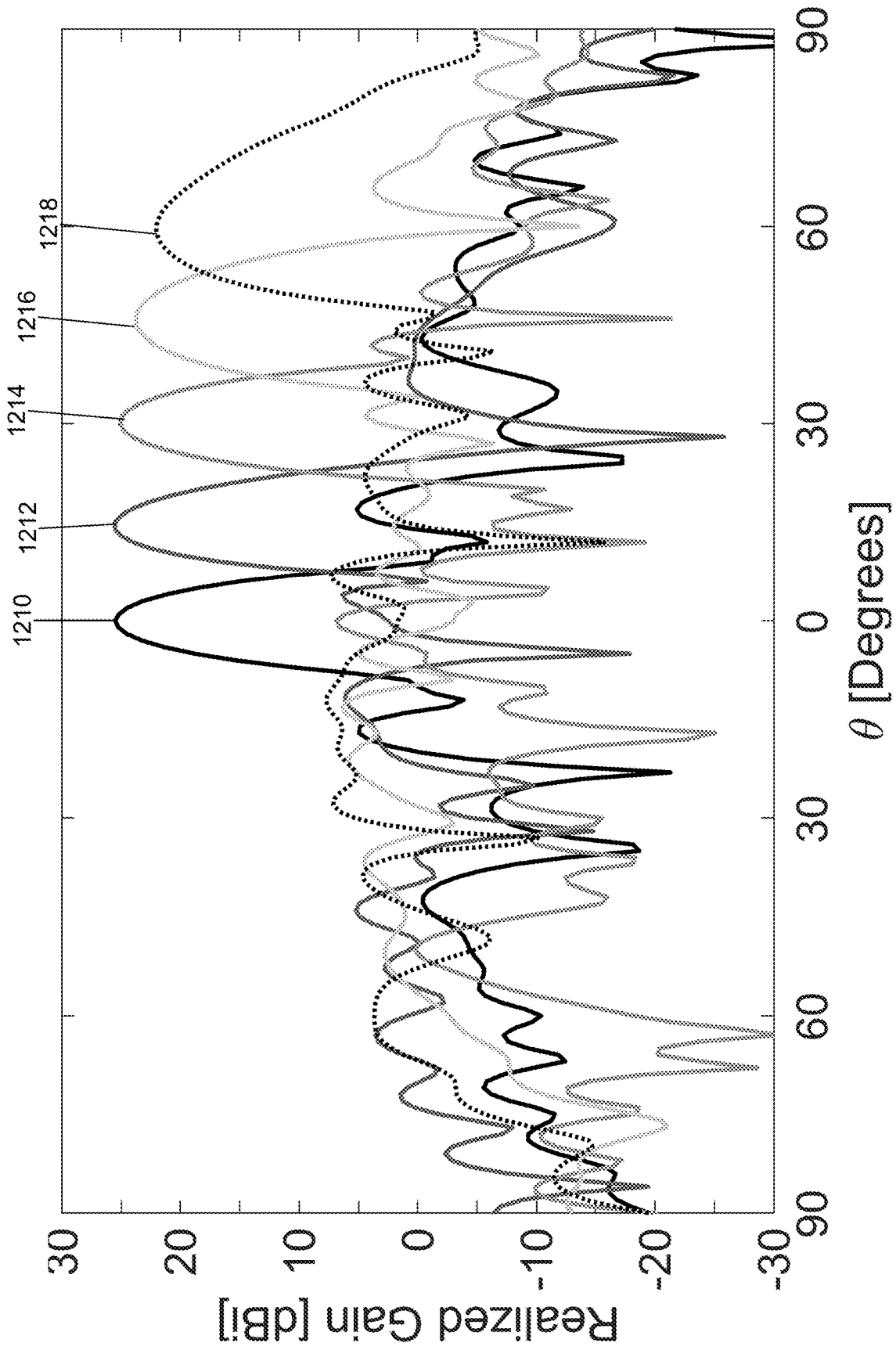


FIG. 12B

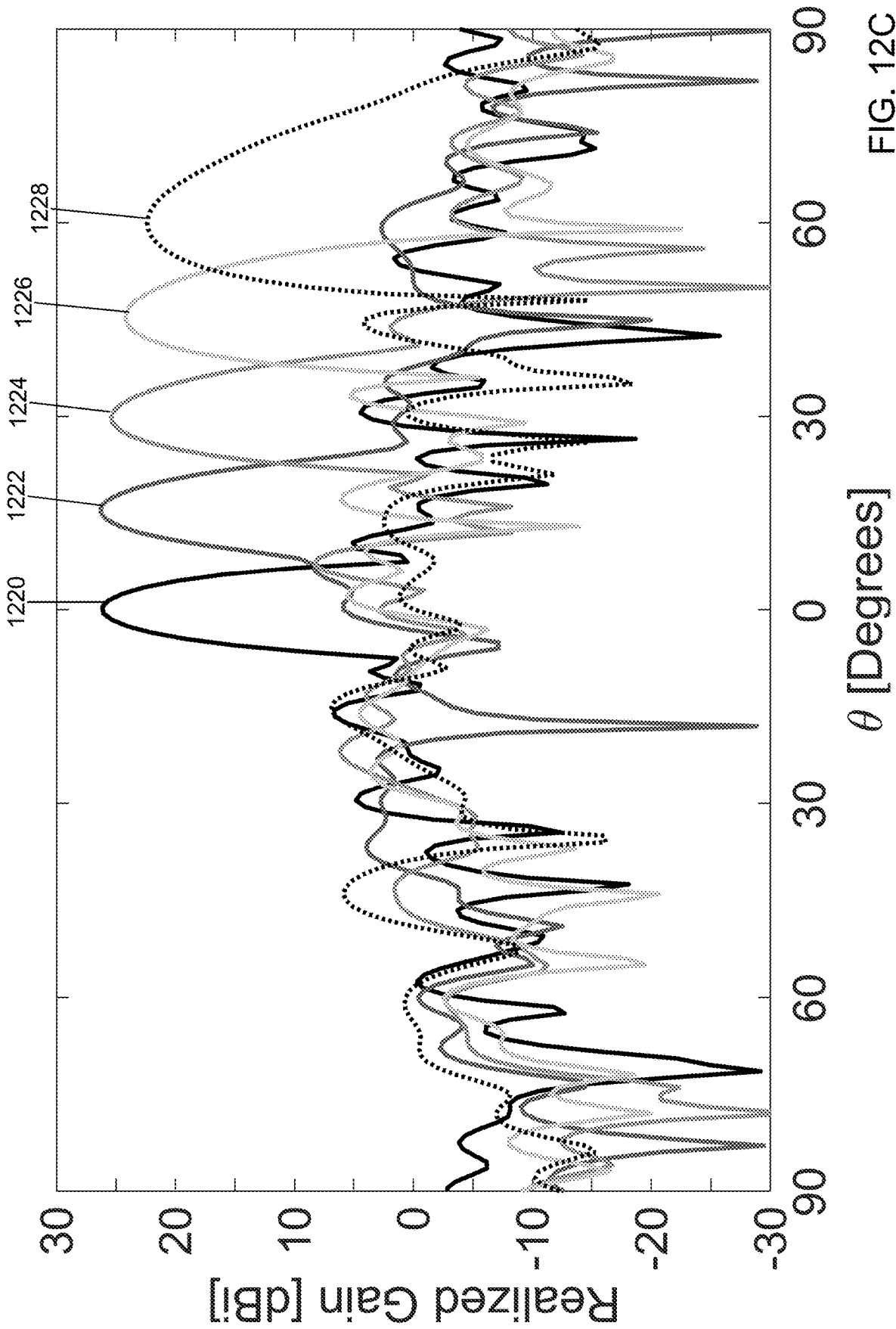


FIG. 12C

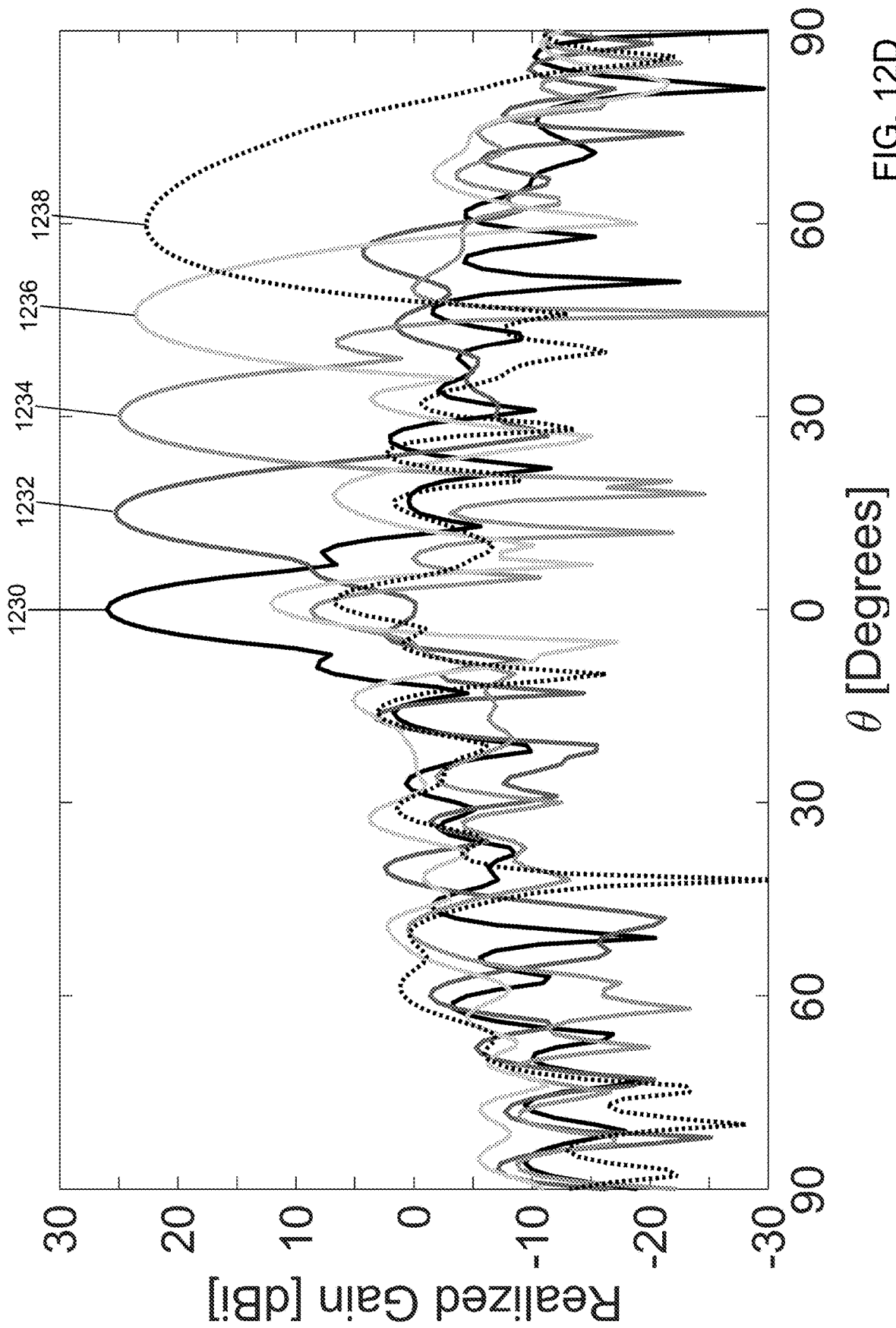


FIG. 12D

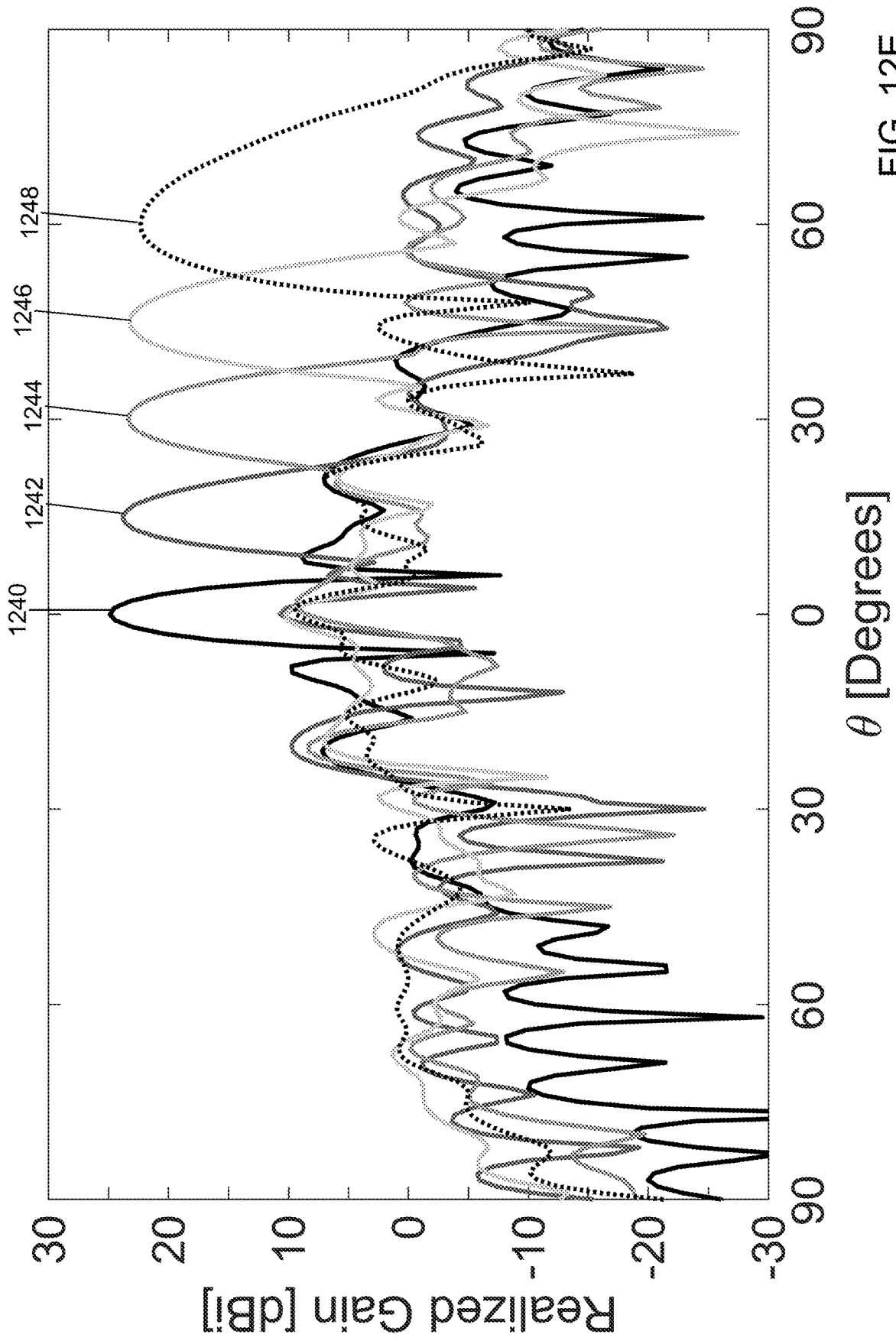


FIG. 12E

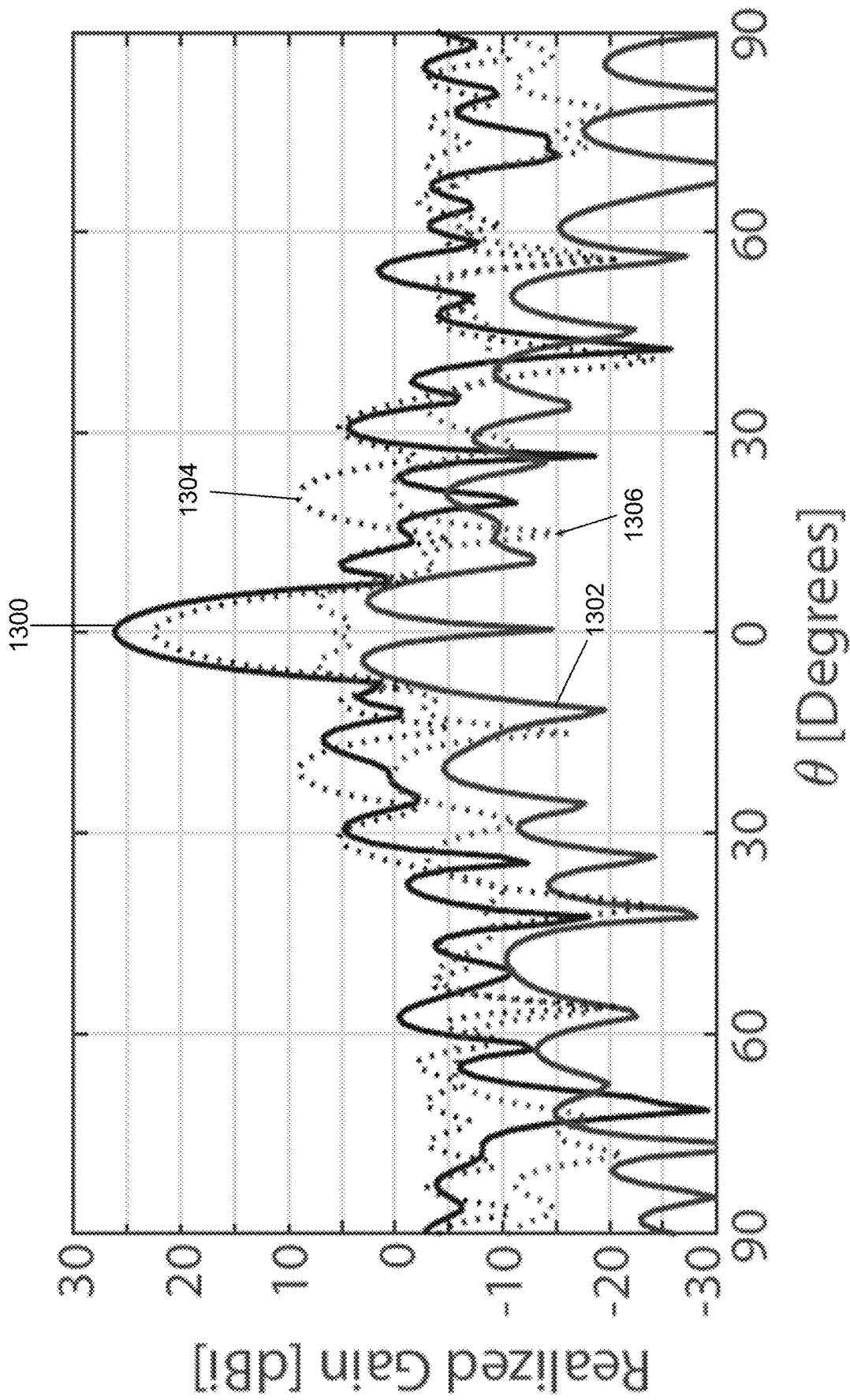


FIG. 13

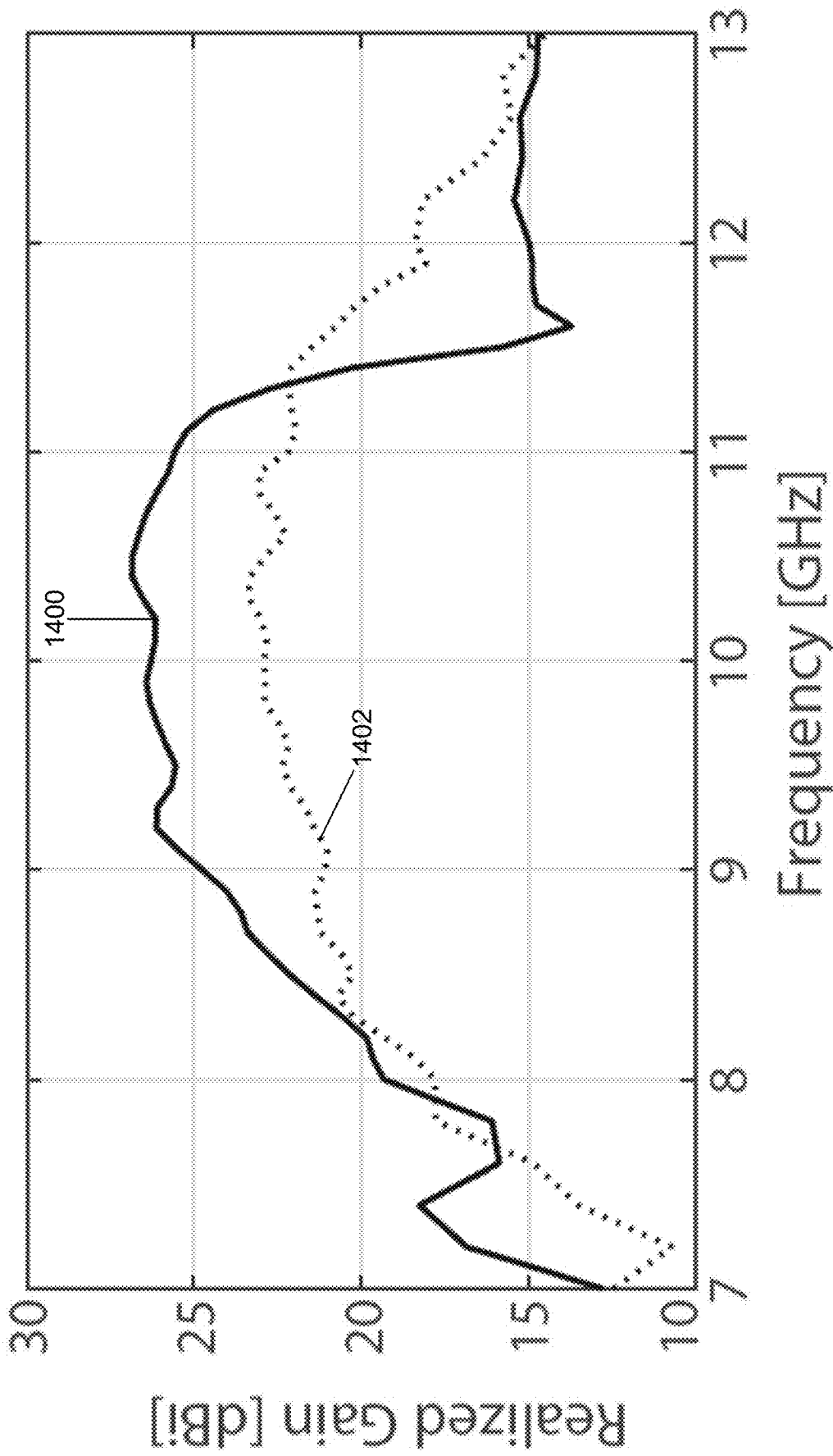


FIG. 14

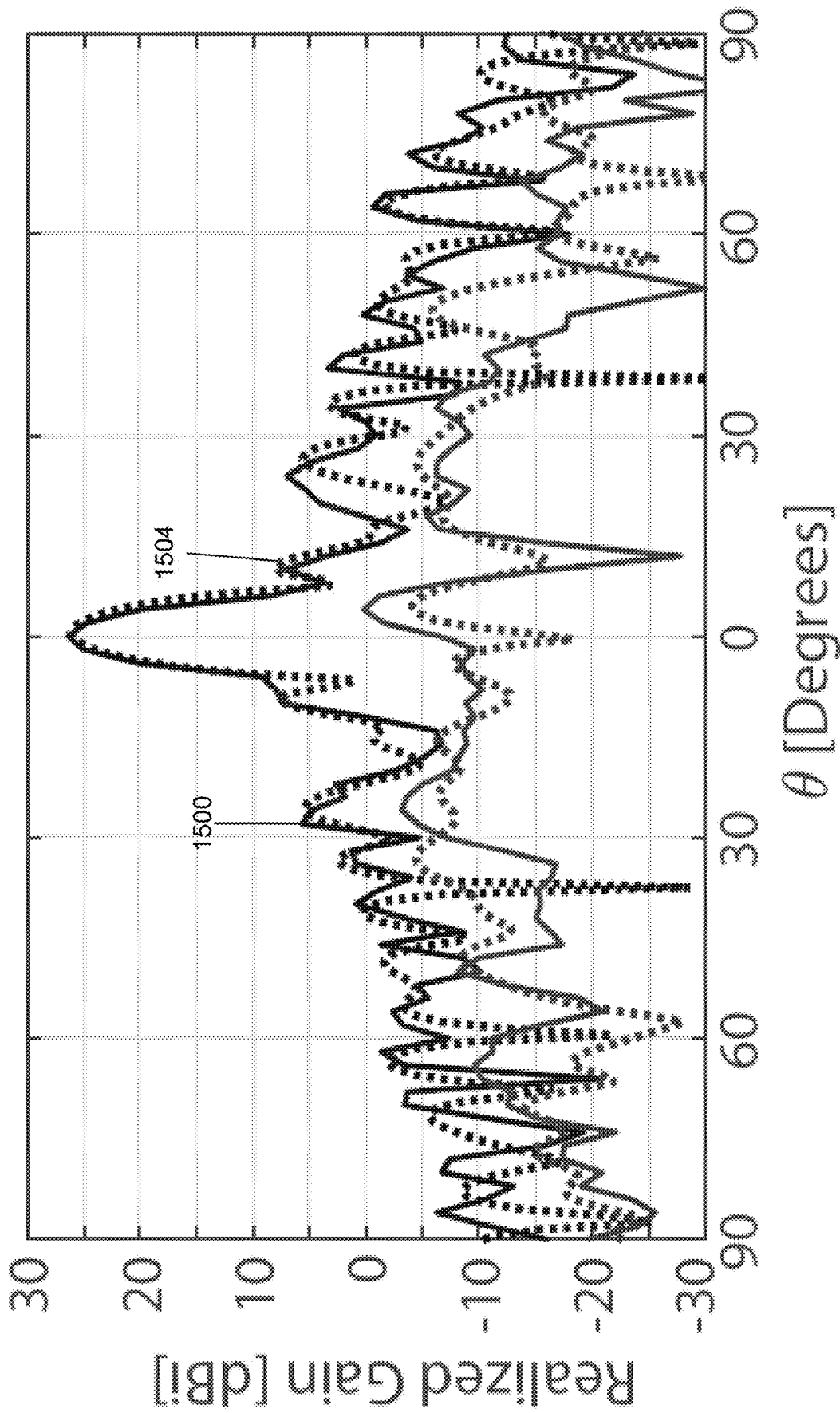


FIG. 15A

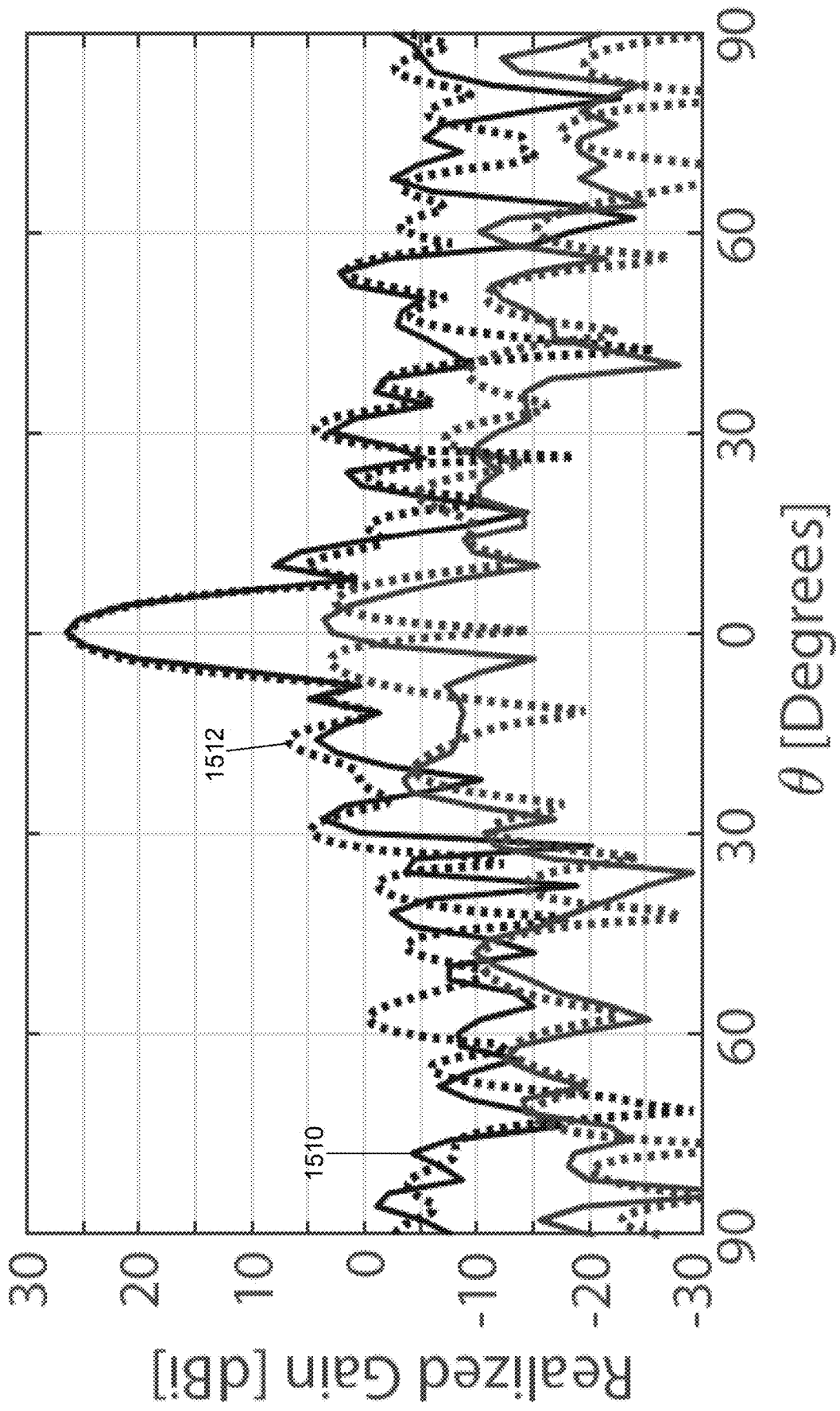


FIG. 15B

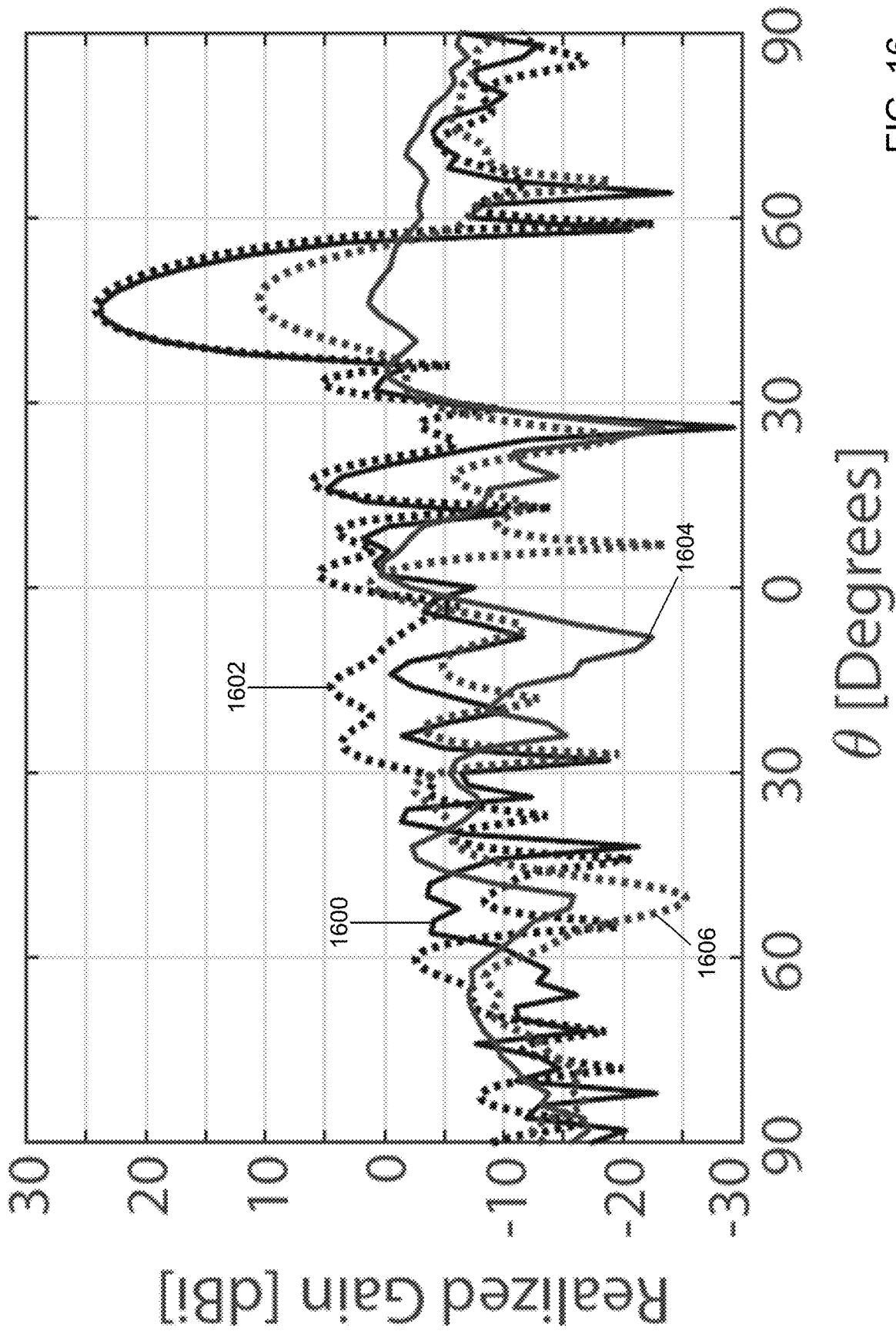


FIG. 16

2-BIT PHASE QUANTIZATION PHASED ARRAY ELEMENT

REFERENCE TO GOVERNMENT RIGHTS

This invention was made with government support under N00014-16-1-2308 awarded by the US Navy/ONR. The government has certain rights in the invention.

BACKGROUND

A phased array antenna is an array of antennas in which a relative phase of signals feeding each antenna is varied such that an effective radiation pattern of the array is reinforced in a desired direction and suppressed in undesired directions to provide electronic steering of a beam. To convert a reflector array into a beam steerable antenna, a phase shift distribution provided by spatial phase shifting pixels is dynamically changed depending on the direction of the desired output beam in the far field.

Beams are formed by shifting the phase of the signal emitted from each radiating element to provide either constructive or destructive interference to steer the beam. These antenna systems come in different sizes and scales due to several factors such as frequency and power requirements. High-power phased array antenna technology that yields an affordable system is a major problem in the commercial and military wireless industry. The cost of current phased array antenna technology is a major factor that limits application to the most expensive military systems. Additionally, the solid-state technology that lies at the heart of current phased array antenna technology has inherent limitations when it comes to power and heat handling capability due to the generation of a large amount of heat.

Reflective array antennas have been increasingly investigated in recent years as affordable solutions to provide beam collimation and adaptive pattern scanning for a wide range of wireless communication systems. A reflective array antenna is typically used to collimate the wave front generated by a low-gain feed antenna. Each unit cell of the reflective array antenna acts as a spatial phase shifter to scatter the incident wave with a specific phase shift to realize a desired phase profile for the reflected wave over the array's aperture to form a high gain pencil beam at an intended direction. The direction of the main beam can be steered by adaptively changing the reflection phase of each array element. Ideally, it is desirable to have the reflective array antenna's unit cells that can be reconfigured to yield any arbitrary phase shift values between 0° and 360° to provide perfect phase correction. However, the reconfiguration techniques to achieve any arbitrary phase shift values between 0° and 360° require changing the control voltage continuously and individually configuring the unit cells, which results in a relatively sophisticated architecture for voltage supply circuitry. Moreover, it is challenging to realize the full, reconfigurable 0° to 360° phase range over a broad frequency range (e.g., with fractional bandwidth of larger than 10%). These limitations reduce the practicality of these reconfiguration techniques for various scenarios where reflective array antennas having large numbers of unit cells and wideband operation are needed. Therefore, instead of fulfilling a continuous 0° to 360° phase range, discrete phase correction schemes that quantize this phase range into a number of discrete levels have been widely adopted in order to reduce the complexity of the control circuitry and increase operating bandwidths of beam-steerable reflective array antennas.

The simplest phase quantization scheme is 1-bit, which has been demonstrated as sufficient for beam scanning operation. The use of only two phase states for reconfigurable unit cells significantly reduces the complexity of the unit cell design and the digital control circuit compared to a phase correction scheme using a higher number of phase states. However, the 1-bit discretization results in a large phase error accumulated over a reflective array antenna's aperture reducing the directivity by about 3.7 decibel (dB) compared to that achieved by a perfectly collimated reflective array antenna. Improving the phase quantization to 2-bit (e.g., four phase states) helps recover about 3 dB of this 3.7-dB directivity reduction, which is a significant improvement. Increasing the number of phase states beyond four yields only a modest increase in the directivity of less than 0.7 dB. This modest increase can be easily canceled by the higher losses due to additional switches and more complicated unit cell designs. Indeed, a number of publications reveal that an average phase shifter loss is about 1 dB/bit. This means adding one more bit to the phase correction scheme generally increases the overall system loss by 1 dB. Taking into account this phase shifter loss, an array using 3-bit phase shifters, while providing about a 0.5 dB higher directivity gain, provides a slightly lower realized gain compared to one using 2-bit phase shifters. In an electronically reconfigurable reflective array antenna, a large fraction of the fabrication cost is often due to the switches (e.g., PIN-diode, MEMS switches) used for reconfiguration. Therefore, moving from a 1-bit to a 2-bit phase quantization scheme for reconfigurable reflective array antennas provides the biggest performance improvement.

SUMMARY

In an illustrative embodiment, a phase shift element is provided. The phase shift element includes, but is not limited to, a first dielectric layer, a conductive layer, a second dielectric layer, a conducting pattern layer, a plurality of switches, and a plurality of vertical interconnect accesses (vias). The first dielectric layer includes a top, first dielectric surface and a bottom, first dielectric surface. The top, first dielectric surface is on an opposite side of the first dielectric layer relative to the bottom, first dielectric surface. The first dielectric layer is formed of a first dielectric material. The conductive layer includes a top conductive surface and a bottom conductive surface. The top conductive surface is on an opposite side of the first conductive layer relative to the bottom conductive surface. The bottom conductive surface is mounted to the top, first dielectric surface. The conductive layer is formed of a first conductive material. The second dielectric layer includes a top, second dielectric surface and a bottom, second dielectric surface. The top, second dielectric surface is on an opposite side of the second dielectric layer relative to the bottom, second dielectric surface. The bottom, second dielectric surface is mounted to the top conductive surface. The second dielectric layer is formed of a second dielectric material. The conducting pattern layer includes a plurality of conductors mounted to the top, second dielectric surface. The conducting pattern layer is formed of a second conductive material. Each conductor of the plurality of conductors is orthogonal to two other conductors of the plurality of conductors. The plurality of switches are mounted to the bottom, first dielectric surface. Each switch of the plurality of switches is configured to be switchable between a conducting position and a non-conducting position. Each vertical interconnect access (via) of the plurality of vias is formed of a third conductive material that extends

through the first dielectric layer, through a third dielectric material formed in and through the conductive layer, and through the second dielectric layer. Each via of the plurality of vias is connected to a single conductor of the plurality of conductors. The first conductive material is configured to reflect an electromagnetic wave incident on the conducting pattern layer and on the second dielectric layer. When a switch of the plurality of switches is in the conducting position, the switch electrically connects two conductors of the plurality of conductors to each other through their respective vias. A plurality of different switch configurations of the plurality of switches provide a 2-bit phase quantization on the reflected electromagnetic wave relative to the electromagnetic wave incident on the conducting pattern layer when the electromagnetic wave is incident on the conducting pattern layer.

In another illustrative embodiment, a phased array antenna is provided. The phased array antenna includes, but is not limited to, a first dielectric layer, a conductive layer, a second dielectric layer, a conducting pattern layer, and a plurality of phase shift elements distributed in a direction. The first dielectric layer includes a top, first dielectric surface and a bottom, first dielectric surface. The top, first dielectric surface is on an opposite side of the first dielectric layer relative to the bottom, first dielectric surface. The first dielectric layer is formed of a first dielectric material. The conductive layer includes a top conductive surface and a bottom conductive surface. The top conductive surface is on an opposite side of the first conductive layer relative to the bottom conductive surface. The bottom conductive surface is mounted to the top, first dielectric surface. The conductive layer is formed of a first conductive material. The second dielectric layer includes a top, second dielectric surface and a bottom, second dielectric surface. The top, second dielectric surface is on an opposite side of the second dielectric layer relative to the bottom, second dielectric surface. The bottom, second dielectric surface is mounted to the top conductive surface. The second dielectric layer is formed of a second dielectric material.

Each phase shift element of the plurality of phase shift elements comprises a conducting pattern layer, a plurality of switches, and a plurality of vertical interconnect accesses (vias). The conducting pattern layer includes a plurality of conductors mounted to the top, second dielectric surface. The conducting pattern layer is formed of a second conductive material. Each conductor of the plurality of conductors is orthogonal to two other conductors of the plurality of conductors. The plurality of switches is mounted to the bottom, first dielectric surface. Each switch of the plurality of switches is configured to be switchable between a conducting position and a non-conducting position. Each vertical interconnect access (via) of the plurality of vias is formed of a third conductive material that extends through the first dielectric layer, through a third dielectric material formed in and through the conductive layer, and through the second dielectric layer. Each via of the plurality of vias is connected to a single conductor of the plurality of conductors. The first conductive material is configured to reflect an electromagnetic wave incident on the conducting pattern layer and on the second dielectric layer. When a switch of the plurality of switches is in the conducting position, the switch electrically connects two conductors of the plurality of conductors to each other through their respective vias. A plurality of different switch configurations of the plurality of switches provide a 2-bit phase quantization on the reflected electromagnetic wave relative to the electromagnetic wave incident on the conducting pattern layer when the electro-

magnetic wave is incident on the conducting pattern layer. A switch configuration of each phase shift element of the plurality of phase shift elements is selected such that the plurality of phase shift elements generates a main beam of the reflected electromagnetic wave in a preselected direction when the electromagnetic wave is incident on the conducting pattern layer.

Other principal features of the disclosed subject matter will become apparent to those skilled in the art upon review of the following drawings, the detailed description, and the appended claims.

BRIEF DESCRIPTION OF THE DRAWINGS

Illustrative embodiments of the disclosed subject matter will hereafter be described referring to the accompanying drawings, wherein like numerals denote like elements.

FIG. 1 depicts a perspective side view of a 2-bit phase shift element in accordance with an illustrative embodiment.

FIG. 2 depicts a top view of the 2-bit phase shift element of FIG. 1 in accordance with an illustrative embodiment.

FIG. 3 depicts an exploded, perspective side view of the 2-bit phase shift element of FIG. 1 in accordance with an illustrative embodiment.

FIGS. 4A to 4D depict bottom views of the 2-bit phase shift element of FIG. 1 with switches arranged to define a first mode, a second mode, a third mode, and a fourth mode, respectively, in accordance with an illustrative embodiment.

FIG. 4E illustrates an incident electric wave and a corresponding reflected electric wave generated based on the operating mode of the switches of FIGS. 4A to 4D in accordance with an illustrative embodiment.

FIG. 5A depicts simulated y-y and x-y reflection coefficients generated by the 2-bit phase shift element of FIG. 1 operating in the first mode and operating in the second mode in accordance with an illustrative embodiment.

FIG. 5B depicts simulated y-y and x-y reflection coefficients generated by the 2-bit phase shift element of FIG. 1 operating in the third mode and operating in the fourth mode in accordance with an illustrative embodiment.

FIG. 5C depicts simulated phases of the y-y and x-y reflection coefficients generated by the 2-bit phase shift element of FIG. 1 operating in the first mode, the second mode, the third mode, and the fourth mode in accordance with an illustrative embodiment.

FIG. 6A depicts simulated u-u reflection coefficients generated by the 2-bit phase shift element of FIG. 1 operating in the first mode, the second mode, the third mode, and the fourth mode in accordance with an illustrative embodiment.

FIG. 6B depicts simulated u-v reflection coefficients generated by the 2-bit phase shift element of FIG. 1 operating in the first mode, the second mode, the third mode, and the fourth mode in accordance with an illustrative embodiment.

FIG. 6C depicts simulated phases of the u-u reflection coefficients generated by the 2-bit phase shift element of FIG. 1 operating in the first mode, the second mode, the third mode, and the fourth mode in accordance with an illustrative embodiment.

FIG. 7 depicts a side view of a transceiver system that includes the 2-bit phase shift element of FIG. 1 in accordance with an illustrative embodiment.

FIG. 8 depicts a perspective view of the transceiver system of FIG. 7 in accordance with an illustrative embodiment.

FIG. 9A depicts a front perspective view of a fabricated phased array antenna of the transceiver system of FIG. 7 in accordance with an illustrative embodiment.

FIG. 9B depicts a back perspective view of the fabricated phased array antenna of the transceiver system of FIG. 7 in accordance with an illustrative embodiment.

FIG. 10 depicts a side view of the transceiver system of FIG. 7 that includes the 2-bit phase shift element of FIG. 1 and that shows incident and reflective electric and magnetic field planes in accordance with an illustrative embodiment.

FIGS. 11A to 11E depict patterns of a distribution of the switch positions of the 2-bit phase shift elements on the aperture of the reflective array antenna to generate a beam steered to 0°, 15°, 30°, 45°, 60°, respectively, in accordance with an illustrative embodiment, where “bit 00” indicates first switch positions for the first mode, “bit 01” indicates third switch positions for the third mode, “bit 11” indicates second switch positions for the second mode, and “bit 10” indicates fourth switch positions for the fourth mode.

FIG. 12A depicts a simulated realized gain for the distribution patterns of FIGS. 11A to 11E as a function of zenith angle at 9.0 gigahertz (GHz) in accordance with an illustrative embodiment.

FIG. 12B depicts a simulated realized gain for the distribution patterns of FIGS. 11A to 11E as a function of zenith angle at 9.5 GHz in accordance with an illustrative embodiment.

FIG. 12C depicts a simulated realized gain for the distribution patterns of FIGS. 11A to 11E as a function of zenith angle at 10.0 GHz in accordance with an illustrative embodiment.

FIG. 12D depicts a simulated realized gain for the distribution patterns of FIGS. 11A to 11E as a function of zenith angle at 10.5 GHz in accordance with an illustrative embodiment.

FIG. 12E depicts a simulated realized gain for the distribution patterns of FIGS. 11A to 11E as a function of zenith angle at 11 GHz in accordance with an illustrative embodiment.

FIG. 13 depicts a comparison between a simulated radiation pattern computed for 2-bit phase shift elements on the aperture of the reflective array antenna and for 1-bit phase shift elements on the aperture of the reflective array as a function of angle at 10 GHz in accordance with an illustrative embodiment.

FIG. 14 depicts a comparison between a simulated peak gain computed for 2-bit phase shift elements on the aperture of the reflective array antenna and for 1-bit phase shift elements on the aperture of the reflective array as a function of frequency in accordance with an illustrative embodiment.

FIG. 15A depicts a comparison between the simulated and the measured radiation patterns as a function of zenith angle at 10 GHz in the E-plane for a beam centered at 0° in accordance with an illustrative embodiment.

FIG. 15B depicts a comparison between the simulated and the measured radiation patterns as a function of zenith angle at 10 GHz in the H-plane for a beam centered at 0° in accordance with an illustrative embodiment.

FIG. 16 depicts a comparison between the simulated and the measured radiation patterns as a function of zenith angle at 10 GHz in the H-plane for a beam centered at 45° in accordance with an illustrative embodiment.

DETAILED DESCRIPTION

Referring to FIG. 1, a perspective side view of a 2-bit phase shift element 100 is shown in accordance with an illustrative embodiment. Referring to FIG. 2, a top view of 2-bit phase shift element 100 is shown in accordance with an illustrative embodiment. Referring to FIG. 3, an exploded,

perspective side view of 2-bit phase shift element 100 is shown in accordance with an illustrative embodiment. Referring to FIGS. 4A to 4D, a bottom view of 2-bit phase shift element 100 is shown in accordance with an illustrative embodiment with switches arranged to define a first mode, a second mode, a third mode, and a fourth mode, respectively. Each of first mode, second mode, third mode, and fourth mode define a distinct phase state of 2-bit phase shift element 100 as discussed further below. Referring to FIG. 4E, an incident electric wave and a corresponding reflected electric wave generated based on the operating mode of the switches of FIGS. 4A to 4D are illustrated in accordance with an illustrative embodiment.

2-bit phase shift element 100 provides 2-bit phase quantization for a beam-steerable reflective array by exploiting four distinct reflection modes of a unit cell comprised of 2-bit phase shift element 100 to define four distinct phase states. Two of the four modes represent polarization-rotation operation while the other two modes represent non-polarization-rotation operation when the unit cell is illuminated by an x-polarized or a y-polarized incident wave. With a specific phase relation between the four reflection modes, 2-bit phase shift element 100 acts as a 2-bit phase shifter under illumination of an incident wave polarized along a first diagonal direction (u-direction) of 2-bit phase shift element 100 as described further below.

2-bit phase shift element 100 may include a first dielectric layer 102, a conducting layer 104, a second dielectric layer 106, and a conducting pattern layer 107. 2-bit phase shift element 100 can be used as a spatial phase shifter of a single-layer, wideband reflective array antenna. 2-bit phase shift element 100 can be switched between a first configuration defined by first switch positions, a second configuration defined by second switch positions, a third configuration defined by third switch positions, and a fourth configuration defined by fourth switch positions shown in FIGS. 4A to 4D, respectively.

First dielectric layer 102 is formed of one or more dielectric materials that may include foamed polyethylene, solid polyethylene, polyethylene foam, polytetrafluoroethylene, air, air space polyethylene, vacuum, etc. Illustrative dielectric materials include RO4003C laminate and RO3006 laminate sold by Rogers Corporation headquartered in Chandler, Ariz., USA.

Second dielectric layer 106 is also formed of one or more dielectric materials. First dielectric layer 102 and second dielectric layer 106 may be formed of the same or different dielectric materials and the same or a different number of layers of dielectric material.

Conducting layer 104 may be formed of a sheet of conductive material such as copper plated steel, silver plated steel, silver plated copper, silver plated copper clad steel, copper, copper clad aluminum, steel, etc. Conducting layer 104 is a conducting surface with high conductivity that reflects received electromagnetic waves. Conducting layer 104 is connected to a fixed potential that may be, but is not necessarily, a ground potential. Conducting layer 104 may be generally flat or formed of ridges or bumps. For illustration, conducting layer 104 may be formed of a flexible membrane coated with a conductor.

Conducting pattern layer 107 also may be formed of a conductive material such as copper plated steel, silver plated steel, silver plated copper, silver plated copper clad steel, copper, copper clad aluminum, steel, etc. Conducting layer 104 and conducting pattern layer 107 may be formed of the same or a different conductive material.

Conducting layer **104** is mounted between first dielectric layer **102** and second dielectric layer **106** such that a top surface **310** of first dielectric layer **102** is mounted to a bottom surface of conducting layer **104**, and second dielectric layer **106** is mounted to a top surface **312** of conducting layer **104**. Each of first dielectric layer **102**, conducting layer **104**, and second dielectric layer **106** has a generally square top and bottom surface shape in an x-y plane and a thickness in a vertical direction denoted by a z-axis, where an x-axis is perpendicular to a y-axis, and both the x-axis and the y-axis are perpendicular to the z-axis to form a right-handed coordinate 3-dimensional (D) reference frame denoted x-y-z frame **122**. First dielectric layer **102**, conducting layer **104**, and second dielectric layer **106** have a length **120** parallel to the x-axis, and a width **121** parallel to the y-axis. In the illustrative embodiment, length **120** is equal to width **121**.

Second dielectric layer **106** has a back wall **108**, a right-side wall **110**, a front wall **112**, a left-side wall **114**, a top surface **115**, and a bottom surface (not shown). The bottom surface of second dielectric layer **106** is mounted to top surface **312** of conducting layer **104** though again second dielectric layer **106** may be formed of a plurality of dielectric layers such that a bottom layer is mounted to top surface **312** of conducting layer **104**.

The top and bottom surfaces of each of first dielectric layer **102**, conducting layer **104**, and second dielectric layer **106** are generally flat. First dielectric layer **102** has a first thickness **116** parallel to the z-axis. Conducting layer **104** has a second thickness **117** parallel to the z-axis. Second dielectric layer **106** has a third thickness **118** parallel to the z-axis.

Conducting pattern layer **107** is formed on top surface **115** of second dielectric layer **106** opposite conducting layer **104** though again second dielectric layer **106** may be formed of a plurality of dielectric layers such that conducting pattern layer **107** is mounted to top surface **312** of a top layer of second dielectric layer **106**. Conducting pattern layer **107** includes a first corner conductor **124a**, a second corner conductor **124b**, a third corner conductor **124c**, and a fourth corner conductor **124d**. In the illustrative embodiment, first corner conductor **124a**, second corner conductor **124b**, third corner conductor **124c**, and fourth corner conductor **124d** each form an open arrow shape with arrow tip arms separated by 90 degrees and each arrow tip pointed at 135°, 45°, 315°, and 225°, respectively, in the x-y plane and relative to the +x-direction. Thus, a tip of each open arrow shape is pointed in a direction that is rotated 90° relative to each adjacent tip.

First corner conductor **124a**, second corner conductor **124b**, third corner conductor **124c**, and fourth corner conductor **124d** are symmetrically distributed relative to each corner of top surface **115** of second dielectric layer **106**. First corner conductor **124a** and second corner conductor **124b** form a mirror image of third corner conductor **124c** and fourth corner conductor **124d** relative to an x-z center plane through a center **134** of top surface **115** of second dielectric layer **106**. The x-z center plane is parallel to the x-z plane defined by x-y-z frame **122**. First corner conductor **124a** and fourth corner conductor **124d** form a mirror image of second corner conductor **124b** and third corner conductor **124c** relative to a y-z center plane through center **134** of top surface **115** of second dielectric layer **106**. The y-z center plane is parallel to the y-z plane defined by x-y-z frame **122**.

First corner conductor **124a** is positioned in an upper left quadrant of top surface **115** of second dielectric layer **106**. First corner conductor **124a** includes a first connecting arm **128a**, a first x-arm **130a**, and a first y-arm **132a**. First x-arm

130a and first y-arm **132a** are perpendicular to each other. First connecting arm **128a** is parallel to a v-axis where $v=-x+y$, as shown by an x-y-u-v 2-D reference frame **210**. First x-arm **130a** and first y-arm **132a** are joined to form the arrowhead shape in an upper left corner **136** pointed in the v-axis direction, and first connecting arm **128a** is joined to first x-arm **130a** and first y-arm **132a** to form the shaft that extends from the arrowhead shape toward center **134**. As a result, first connecting arm **128a** is aligned with and extends from the tip formed at the intersection of first x-arm **130a** and first y-arm **132a**. First connecting arm **128a**, first x-arm **130a**, and first y-arm **132a** are used to describe a shape of first corner conductor **124a** and typically are not distinct elements but form a single conductive structure.

A first vertical interconnect access (via) **302a** connects to first corner conductor **124a** adjacent an edge of first connecting arm **128a** closest to center **134**. First connecting arm **128a** connects first x-arm **130a** and first y-arm **132a** to first via **302a**. First connecting arm **128a** extends parallel to a second diagonal axis defined by the v-axis between center **134** and upper left corner **136**. The first diagonal axis defined by a u-axis is perpendicular to the second diagonal axis, the v-axis, and both the u-axis and the v-axis are perpendicular to the z-axis to form a right-handed coordinate 3-D reference frame denoted a u-v-z frame. First x-arm **130a** extends from upper left corner **136** towards an upper right corner **138** parallel to the x-axis. First y-arm **132a** extends from upper left corner **136** towards a lower left corner **142** parallel to the y-axis.

First x-arm **130a** is a first distance **200** from back wall **108**. First y-arm **132a** is first distance **200** from left-side wall **114**. First x-arm **130a** has a corner arm length **202** and a corner arm width **204**. First y-arm **132a** has corner arm length **202** and corner arm width **204**. First connecting arm **128a** has an arm length **208** and an arm width **206**. For simplicity of description, first x-arm **130a**, first y-arm **132a**, and first connecting arm **128a** have been described to overlap near an upper left corner **136** though again first connecting arm **128a**, first x-arm **130a**, and first y-arm **132a** typically are not distinct elements, but form a single conductive structure.

First via **302a** forms an electrical connection between first connecting arm **128a** and a first throw arm **306** of a first switch (not shown) and a fourth throw arm **309** of a fourth switch (not shown) through first dielectric layer **102**, conducting layer **104**, and second dielectric layer **106** to form an electronic circuit. First via **302a** is formed of a conductive material. A first dielectric patch **300a** is formed through conducting layer **104** of a dielectric material. First via **302a** extends generally parallel to the z-axis through first dielectric patch **300a**.

Second corner conductor **124b** is positioned in an upper right quadrant of top surface **115** of second dielectric layer **106**. Second corner conductor **124b** includes a second connecting arm **128b**, a second x-arm **130b**, and a second y-arm **132b**. Second x-arm **130b** and second y-arm **132b** are perpendicular to each other. Second connecting arm **128b** is parallel to the u-axis where $u=x+y$, as shown by x-y-u-v frame **210**. Second x-arm **130b** and second y-arm **132b** are joined to form the arrowhead shape in upper right corner **138** pointed in the u-axis direction, and second connecting arm **128b** is joined to second x-arm **130b** and second y-arm **132b** to form the shaft that extends from the arrowhead shape toward center **134**. As a result, second connecting arm **128b** is aligned with and extends from the tip formed at the intersection of second x-arm **130b** and second y-arm **132b**. Second connecting arm **128b**, second x-arm **130b**, and

second y-arm **132b** are used to describe a shape of second corner conductor **124b** and typically are not distinct elements but form a single conductive structure.

A second via **302b** connects to second corner conductor **124b** adjacent an edge of second connecting arm **128b** closest to center **134**. Second connecting arm **128b** connects second x-arm **130b** and second y-arm **132b** to second via **302b**. Second connecting arm **128b** extends parallel to the u-axis between center **134** and upper right corner **138**. Second x-arm **130b** extends from upper right corner **138** towards upper left corner **136** parallel to the x-axis. Second y-arm **132b** extends from upper right corner **138** towards a lower right corner **140** parallel to the y-axis.

Second x-arm **130b** is first distance **200** from back wall **108**. Second y-arm **132b** is first distance **200** from right-side wall **110**. Second x-arm **130b** has corner arm length **202** and corner arm width **204**. Second y-arm **132b** has corner arm length **202** and corner arm width **204**. Second connecting arm **128b** has arm length **208** and arm width **206**. For simplicity of description, second x-arm **130b**, second y-arm **132b**, and second connecting arm **128b** have been described to overlap near upper right corner **138** though again second connecting arm **128b**, second x-arm **130b**, and second y-arm **132b** typically are not distinct elements, but form a single conductive structure.

Second via **302b** forms an electrical connection between first throw arm **306** of the first switch and a second throw arm **307** of a second switch (not shown) through first dielectric layer **102**, conducting layer **104**, and second dielectric layer **106** to form an electronic circuit. Second via **302b** is formed of a conductive material. A second dielectric patch **300b** is formed through conducting layer **104** of a dielectric material. Second via **302b** extends generally parallel to the z-axis through second dielectric patch **300b**.

Third corner conductor **124c** is positioned in a lower right quadrant of top surface **115** of second dielectric layer **106**. Third corner conductor **124c** includes a third connecting arm **128c**, a third x-arm **130c**, and a third y-arm **132c**. Third x-arm **130c** and third y-arm **132c** are perpendicular to each other. Third connecting arm **128c** is parallel to the v-axis, as shown by x-y-u-v frame **210**. Third x-arm **130c** and third y-arm **132c** are joined to form the arrowhead shape in lower right corner **140** pointed in the -v-axis direction, and third connecting arm **128c** is joined to third x-arm **130c** and third y-arm **132c** to form the shaft that extends from the arrowhead shape toward center **134**. As a result, third connecting arm **128c** is aligned with and extends from the tip formed at the intersection of third x-arm **130c** and third y-arm **132c**. Third connecting arm **128c** and first connecting arm **128a** are parallel to each other. Third connecting arm **128c**, third x-arm **130c**, and third y-arm **132c** are used to describe a shape of third corner conductor **124c** and typically are not distinct elements but form a single conductive structure.

A third via **302c** connects to third corner conductor **124c** adjacent an edge of third connecting arm **128c** closest to center **134**. Third connecting arm **128c** connects third x-arm **130c** and third y-arm **132c** to third via **302c**. Third connecting arm **128c** extends parallel to the v-axis between center **134** and lower right corner **140**. Third x-arm **130c** extends from lower right corner **140** towards lower left corner **142** parallel to the x-axis. Third y-arm **132c** extends from lower right corner **140** towards upper right corner **138** parallel to the y-axis.

Third x-arm **130c** is first distance **200** from front wall **112**. Third y-arm **132c** is first distance **200** from right-side wall **110**. Third x-arm **130c** has corner arm length **202** and corner arm width **204**. Third y-arm **132c** has corner arm length **202**

and corner arm width **204**. Third connecting arm **128c** has arm length **208** and arm width **206**. For simplicity of description, third x-arm **130c**, third y-arm **132c**, and third connecting arm **128c** have been described to overlap near lower right corner **140** though again third connecting arm **128c**, third x-arm **130c**, and third y-arm **132c** typically are not distinct elements, but form a single conductive structure.

Third via **302c** forms an electrical connection between second throw arm **307** of the second switch and a third throw arm **308** of a third switch (not shown) through first dielectric layer **102**, conducting layer **104**, and second dielectric layer **106** to form an electronic circuit. Third via **302c** is formed of a conductive material. A third dielectric patch **300c** is formed through conducting layer **104** of a dielectric material. Third via **302c** extends generally parallel to the z-axis through third dielectric patch **300c**.

Fourth corner conductor **124d** is positioned in a lower left quadrant of top surface **115** of second dielectric layer **106**. Fourth corner conductor **124d** includes a fourth connecting arm **128d**, a fourth x-arm **130d**, and a fourth y-arm **132d**. Fourth x-arm **130d** and fourth y-arm **132d** are perpendicular to each other. Fourth connecting arm **128d** is parallel to the u-axis, as shown by x-y-u-v frame **210**. Fourth x-arm **130d** and fourth y-arm **132d** are joined to form the arrowhead shape in lower left corner **142** pointed in the -u-axis direction, and fourth connecting arm **128d** is joined to fourth x-arm **130d** and fourth y-arm **132d** to form the shaft that extends from the arrowhead shape toward center **134**. As a result, fourth connecting arm **128d** is aligned with and extends from the tip formed at the intersection of fourth x-arm **130d** and fourth y-arm **132d**. Fourth connecting arm **128d** and second connecting arm **128b** are parallel to each other. Fourth connecting arm **128d**, fourth x-arm **130d**, and fourth y-arm **132d** are used to describe a shape of fourth corner conductor **124d** and typically are not distinct elements but form a single conductive structure.

A fourth via **302d** connects to fourth corner conductor **124d** adjacent an edge of fourth connecting arm **128d** closest to center **134**. Fourth connecting arm **128d** connects fourth x-arm **130d** and fourth y-arm **132d** to fourth via **302d**. Fourth connecting arm **128d** extends parallel to the u-axis between center **134** and lower left corner **142**. Fourth x-arm **130d** extends from lower left corner **142** towards lower right corner **140** parallel to the x-axis. Fourth y-arm **132c** extends from lower left corner **142** towards upper left corner **136** parallel to the y-axis.

Fourth x-arm **130d** is first distance **200** from front wall **112**. Fourth y-arm **132d** is first distance **200** from left-side wall **114**. Fourth x-arm **130d** has corner arm length **202** and corner arm width **204**. Fourth y-arm **132d** has corner arm length **202** and corner arm width **204**. Fourth connecting arm **128d** has arm length **208** and arm width **206**. For simplicity of description, fourth x-arm **130d**, fourth y-arm **132d**, and fourth connecting arm **128d** have been described to overlap near lower left corner **142** though again fourth connecting arm **128d**, fourth x-arm **130d**, and fourth y-arm **132d** typically are not distinct elements, but form a single conductive structure.

Fourth via **302d** forms an electrical connection between third throw arm **308** of the third switch and fourth throw arm **309** of the fourth switch through first dielectric layer **102**, conducting layer **104**, and second dielectric layer **106** to form an electronic circuit. Fourth via **302d** is formed of a conductive material. A fourth dielectric patch **300d** is formed through conducting layer **104** of a dielectric material. Fourth via **302d** extends generally parallel to the z-axis through fourth dielectric patch **300d**.

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Inclusion of first x-arms **130a**, **130b**, **130c**, **130d** perpendicular to first y-arms **132a**, **132b**, **132c**, **132d**, respectively, allows 2-bit phase shift element **100** to support polarizations parallel to the x-axis as well as the y-axis.

Each of the first switch, the second switch, the third switch, and the fourth switch may be single pole, single throw (SPST) switches or electrical structures that act as a SPST switch. Each of the first switch, the second switch, the third switch, and the fourth switch are mounted to bottom surface **400** of first dielectric layer **102** though again first dielectric layer **102** may be formed of a plurality of dielectric layers such that the first switch, the second switch, the third switch, and the fourth switch are mounted to bottom surface **400** of a bottom layer of first dielectric layer **102**. Each of the first switch, the second switch, the third switch, and the fourth switch form switchable connections that have two states: short referred to as a conducting position and open referred to as a non-conducting position.

In a first position, first throw arm **306** of the first switch is closed to electrically connect first via **302a** with second via **302b**. In a second position, first throw arm **306** of the first switch is open to electrically disconnect first via **302a** from second via **302b**. In a first position, second throw arm **307** of the second switch is closed to electrically connect second via **302b** with third via **302c**. In a second position, first throw arm **306** of the second switch is open to electrically disconnect second via **302b** from third via **302c**. In a first position, third throw arm **308** of the third switch is closed to electrically connect third via **302c** with fourth via **302d**. In a second position, third throw arm **308** of the third switch is open to electrically disconnect third via **302c** from fourth via **302d**. In a first position, fourth throw arm **309** of the fourth switch is closed to electrically connect fourth via **302d** with first via **302a**. In a second position, fourth throw arm **309** of the fourth switch is open to electrically disconnect fourth via **302d** from first via **302a**.

When only first throw arm **306** of the first switch and second throw arm **307** of the second switch are in the first position as shown in FIG. 4A, 2-bit phase shift element **100** may be designated as in a “bit 00” configuration also referred to as the first configuration defined by first switch positions, as a first mode, or as a first phase state of 2-bit phase shift element **100**. When only first throw arm **306** of the first switch and fourth throw arm **309** of the fourth switch are in the first position as shown in FIG. 4B, 2-bit phase shift element **100** may be designated as in a “bit 11” configuration also referred to as the second configuration defined by second switch positions, as a second mode, or as a second phase state of 2-bit phase shift element **100**. When first throw arm **306** of the first switch, second throw arm **307** of the second switch, third throw arm **308** of the third switch, and fourth throw arm **309** of the fourth switch are all in the first position as shown in FIG. 4C, 2-bit phase shift element **100** may be designated as in a “bit 01” configuration also referred to as the third configuration defined by third switch positions, as a third mode, or as a third phase state of 2-bit phase shift element **100**. When first throw arm **306** of the first switch, second throw arm **307** of the second switch, third throw arm **308** of the third switch, and fourth throw arm **309** of the fourth switch are all in the second position as shown in FIG. 4D, 2-bit phase shift element **100** may be designated as in a “bit 10” configuration also referred to as the fourth configuration defined by fourth switch positions,

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as a fourth mode, or as a fourth phase state of 2-bit phase shift element **100**. Of course, the modes can be defined in other manners to distinguish the four operating modes of 2-bit phase shift element **100**.

A combined electrical path length of first connecting arm **128a** and first via **302a** is approximately $\lambda_0/4$ (a quarter of the wavelength) and includes arm length **208** that defines a length of first connecting arm **128a** and third thickness **118**, third thickness **117**, and third thickness **116** that define a length of first via **302a**. Similarly, a combined electrical path length of second connecting arm **128b** and second via **302b** is approximately $\lambda_0/4$. Similarly, a combined electrical path length of third connecting arm **128c** and third via **302c** is approximately $\lambda_0/4$. Similarly, a combined electrical path length of fourth connecting arm **128d** and fourth via **302d** is approximately $\lambda_0/4$. λ_0 is the wavelength in free space at the frequency of operation.

An electrical path length of each of first throw arm **306** of the first switch, second throw arm **307** of the second switch, third throw arm **308** of the third switch, and fourth throw arm **309** of the fourth switch can be set in the range from $\lambda_0/100$ to $\lambda_0/5$ (e.g. based on a range of physical dimensions of several commercial electronic switches and PIN diodes). The electrical path length for the currents is included in a total electrical path length for each connected pair of arms (e.g., first connecting arm **128a** and first via **302a** connected to second via **302b** and second connecting arm **128b** by first throw arm **306** of the first switch) when connected by a throw arm of one of the switches. The total electrical path length of each connected pair of arms is approximately half a wavelength.

Referring to FIG. 4E, a reflection coefficient matrix includes four elements describing the transfer coefficients from an incident electric field (having either an x- or y-polarization) to a reflected electric field (having either an x- or y-polarization). Among the four reflection modes, two modes represent polarization rotation operation (e.g., $|R_{xy}|=|R_{yx}|=1$) with relative reflection phase values of 0° and 180° . The other two modes represent non-polarization-rotation operation (e.g., $|R_{xx}|=|R_{yy}|=1$) with relative phase values of 90° and 270° . These four reflection modes provide reflected waves having the same polarization and four phase states with a 90° progression when 2-bit phase shift element **100** is illuminated with an incident wave polarized along either of its two diagonal directions. 2-bit phase shift element **100** provides 2-bit phase quantization by exploiting the four distinct reflection modes. These four reflection modes can be characterized by the corresponding reflection coefficient matrices

$$R^{(1)} = \begin{bmatrix} R_{xx} & R_{xy} \\ R_{yx} & R_{yy} \end{bmatrix} = \begin{bmatrix} 0 & 1e^{j0^\circ} \\ 1e^{j0^\circ} & 0 \end{bmatrix},$$

$$R^{(2)} = \begin{bmatrix} R_{xx} & R_{xy} \\ R_{yx} & R_{yy} \end{bmatrix} = \begin{bmatrix} 0 & 1e^{j180^\circ} \\ 1e^{j180^\circ} & 0 \end{bmatrix},$$

$$R^{(3)} = \begin{bmatrix} R_{xx} & R_{xy} \\ R_{yx} & R_{yy} \end{bmatrix} = \begin{bmatrix} 1e^{j90^\circ} & 0 \\ 0 & 1e^{j90^\circ} \end{bmatrix},$$

$$R^{(4)} = \begin{bmatrix} R_{xx} & R_{xy} \\ R_{yx} & R_{yy} \end{bmatrix} = \begin{bmatrix} 1e^{j270^\circ} & 0 \\ 0 & 1e^{j270^\circ} \end{bmatrix},$$

where $R^{(1)}$ is the reflection coefficient matrix for the first mode, $R^{(2)}$ is the reflection coefficient matrix for the second

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mode, $R^{(3)}$ is the reflection coefficient matrix for the third mode, and $R^{(4)}$ is the reflection coefficient matrix for the fourth mode.

In $R^{(1)}$, $R^{(2)}$, $R^{(3)}$, and $R^{(4)}$,

$$R_{ij} = \frac{E_i^{ref}}{E_j^{inc}},$$

where E_i^{ref} is the reflected electric field intensity along the i direction, and E_j^{inc} is the incident electric field intensity along the j direction ($i, j = x$ or y). When illuminated with an incident wave polarized along the x -axis or the y -axis, 2-bit phase shift element **100** switched into one of the first two reflection modes (Mode 1 (the first mode) and Mode 2 (the second mode)) rotates the polarization of the reflected field by $+90^\circ$ and -90° with respect to that of the incident electric field, creating a 180° phase difference in the reflected electric field in these two modes of operation. The polarization rotation operation of the two modes are characterized by $|R_{yy}^{(1)}| = |R_{xx}^{(1)}| = |R_{xy}^{(2)}| = |R_{yx}^{(2)}| = 1$ and $|R_{xx}^{(1)}| = |R_{yy}^{(1)}| = |R_{xx}^{(2)}| = |R_{yy}^{(2)}| = 0$.

In the other two reflection modes (Mode 3 (the third mode) and Mode 4 (the fourth mode)), 2-bit phase shift element **100** maintains the polarization of the reflected electric field with respect to the x -polarized or y -polarized incident field due to $|R_{yy}^{(3)}| = |R_{xx}^{(3)}| = |R_{yy}^{(4)}| = |R_{xx}^{(4)}| = 0$ and $|R_{xx}^{(3)}| = |R_{yy}^{(3)}| = |R_{xx}^{(4)}| = |R_{yy}^{(4)}| = 1$ and provides a phase difference of 180° between the reflected electric fields of these two modes. Additionally, the phase difference between the corresponding dominant reflection coefficients of a polarization-rotating mode (e.g., $R_{xy}^{(1)}$, $R_{yx}^{(1)}$, $R_{xy}^{(2)}$, or $R_{yx}^{(2)}$) and a non-polarization-rotating mode (e.g., $R_{xx}^{(3)}$, $R_{yy}^{(3)}$, $R_{xx}^{(4)}$, or $R_{yy}^{(4)}$) is either 90° or 270° .

2-bit phase shift element **100** having these four reflection modes can provide 2-bit phase quantization for the reflected electric fields when illuminated with an incident electric field polarized along the direction of

$$\hat{u} = \frac{1}{\sqrt{2}}(\hat{x} + \hat{y})$$

or

$$\hat{v} = \frac{1}{\sqrt{2}}(-\hat{x} + \hat{y}).$$

Assuming the incident electric field vector has the form $\vec{E}^{inc} = \hat{u}E_0e^{j\Phi} = \hat{x}E_x^{inc} + \hat{y}E_y^{inc}$, where

$$E_x^{inc} = E_y^{inc} = \frac{1}{\sqrt{2}}E_0e^{j\Phi},$$

the reflected electric field vector produced by 2-bit phase shift element **100** in the four modes of operation can be written as follows:

$$\vec{E}^{ref,(1)} = \hat{x}E_y^{inc}R_{xy}^{(1)} + \hat{y}E_x^{inc}R_{yx}^{(1)} = \frac{1}{\sqrt{2}}E_0e^{j\Phi}e^{j90^\circ}(\hat{x} + \hat{y}) = E_0e^{j\Phi}\hat{u}, \quad (1)$$

$$\vec{E}^{ref,(2)} = \quad (2)$$

$$\hat{x}E_y^{inc}R_{xy}^{(2)} + \hat{y}E_x^{inc}R_{yx}^{(2)} = \frac{1}{\sqrt{2}}E_0e^{j\Phi}e^{j180^\circ}(\hat{x} + \hat{y}) = E_0e^{j(\Phi+180^\circ)}\hat{u}, \quad (3)$$

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-continued

$$\vec{E}^{ref,(3)} = \hat{x}E_y^{inc}R_{xy}^{(3)} + \hat{y}E_x^{inc}R_{yx}^{(3)} = \frac{1}{\sqrt{2}}E_0e^{j\Phi}e^{j90^\circ}(\hat{x} - \hat{y}) = E_0e^{j(\Phi+90^\circ)}\hat{u}, \quad (4)$$

$$\vec{E}^{ref,(4)} = \quad (5)$$

$$\hat{x}E_y^{inc}R_{xy}^{(4)} + \hat{y}E_x^{inc}R_{yx}^{(4)} = \frac{1}{\sqrt{2}}E_0e^{j\Phi}e^{j270^\circ}(\hat{x} + \hat{y}) = E_0e^{j(\Phi+270^\circ)}\hat{u}.$$

Equations (1)-(4) show that the reflected electric fields are polarized along the u -axis in all four cases with the relative phase values of 0° (Mode 1), 90° (Mode 3), 180° (Mode 2), and 270° (Mode 4). Therefore, the four operating modes or phase states of 2-bit phase shift element **100** provide a 2-bit phase quantization for the reflected electromagnetic field.

FIG. 4E illustrates the operation of the four reflection modes in their interaction with the incident, linearly-polarized electric field $\vec{E}^{inc} = \hat{u}E_0e^{j\Phi}$, where Φ may be chosen to be -45° for convenience. Mode 1 rotates the x -component and the y -component of the incident electric field into the y -component and the x -component of the reflected electric field, respectively, with a 0° phase shift. As a result, the total reflected electric field vector is the same as the total incident electric field vector. Mode 2 also rotates the x -component and the y -component of the incident electric field into the y -component and the x -component of the reflected electric field, respectively, but with a 180° phase shift, providing the total reflected field vector in the opposite direction of the incident electric field vector. As a result, Modes 1 and 2 create two relative phase values of 0° and 180° .

Mode 3 reflects the x -component and the y -component of the incident electric field with the same polarization and a 90° phase shift. Mode 4 reflects the x -component and the y -component of the incident electric field with the same polarization and a 270° phase shift. Since the phase shifts added to the reflected electric field component in the x -component and the y -component are equal in the third mode and the fourth mode, the resulting reflected electric field maintains its polarization along the u -axis like the incident field. However, the phase leads by the reflected electric fields of 90° and 270° in Modes 3 and 4, respectively, compared to that in Mode 1. Therefore, the four reflection modes provide reflected fields having the same polarization along the u -axis with relative phase values of 0° , 90° , 180° , and 270° creating 2-bit phase shifts.

The four reflection modes of 2-bit phase shift element **100** are defined by four configurations of the switches as shown in FIGS. 4A to 4D. When three of the vias are electrically connected to each other using two ON switches (shown as Mode 1 in FIG. 4A or Mode 2 in FIG. 4B by first throw arm **306** of the first switch being closed and either second throw arm **307** of the second switch being closed or fourth throw arm **309** of the fourth switch being closed), 2-bit phase shift element **100** acts as a polarization rotator when illuminated with an incident wave having linear polarization along the x -axis or y -axis. When a corner conductor **124a**, **124b**, **124c**, **124d** is connected to another corner conductor **124a**, **124b**, **124c**, **124d** as shown in either FIG. 4A or FIG. 4B, the respective corner conductors are deactivated. When a corner conductor **124a**, **124b**, **124c**, **124d** is not connected to another corner conductor **124a**, **124b**, **124c**, **124d**, the respective corner conductors are activated for polarization rotation operation. Each activated corner conductor **124a**, **124b**, **124c**, **124d** allows strong induced electrical currents to flow on a respective connecting arm **128a**, **128b**, **128c**, **128d** along a diagonal line of 2-bit phase shift element **100** when

it is illuminated with an x-polarized or y-polarized incident wave. If the induced currents are strong along only one diagonal line, 2-bit phase shift element **100** presents a perfect electrical conductor (PEC)-like reflection along this diagonal line and a perfect magnetic conductor (PMC)-like reflection along the perpendicular direction. As a result, the polarization of the reflected wave is rotated by 90° or -90° with respect to the incident wave, depending on which diagonal line has the strong induced currents. These opposite rotation directions create reflected electric field vectors in reversed directions representing a phase difference of 180° in the reflected wave. In Mode 1, the isolated corner conductor is fourth corner conductor **124d**. In Mode 2, the isolated corner conductor is third corner conductor **124c** making Modes 1 and 2 orthogonal to each other.

On the other hand, connecting or isolating all four corner conductors **124a**, **124b**, **124c**, **124d**, as shown for Modes 3 and 4 in FIGS. **4C** and **4D**, respectively, deactivates the polarization rotation operation of 2-bit phase shift element **100**. 2-bit phase shift element **100** in these two modes reflects an x-polarized or y-polarized incident wave while maintaining the same polarization. Moreover, due to rotational symmetry of the connections for Mode 3 or Mode 4, the reflection coefficients R_{xx} and R_{yy} have the same phases and amplitudes. A phase difference of 180° in the co-polarization reflection coefficients of the two non-polarization rotating modes can be achieved by having strong induced currents in both diagonal directions in one mode (Mode 4) while having weak induced currents in both diagonal directions in the other mode (Mode 3). 2-bit phase shift element **100** acts more like a PEC surface in the mode (Mode 4) with strong currents and more like a PMC surface in the mode (Mode 3) with weak currents.

2-bit phase shift element **100** was simulated using the unit cell boundary condition in CST Microwave Studio. 2-bit phase shift element **100** was constructed using three Rogers 4003C substrates bonded together by two layers of Rogers 4450F prepreg. 2-bit phase shift element **100** had a periodicity of 12 millimeters (mm) and was designed to operate at X band. The feature dimensions were tuned to result in four reflection modes that were as close as possible to those characterized by $R^{(1)}$, $R^{(2)}$, $R^{(3)}$, and $R^{(4)}$ at 10 GHz. Subsequently, the conditions on the amplitudes and phases of the reflection coefficients were relaxed and the feature dimensions were further tuned to expand the operating bandwidth as much as possible. The relaxed conditions were defined such that the dominant reflection coefficients of each mode had magnitudes of no less than -1 dB and phases within $\pm 15^\circ$ of the desired phase value. Since the four desired (relative) phase states are 0° , 90° , 180° , and 270° , the relaxed phase condition means that the difference between two consecutive phase state is within the range of 60° - 120° .

Illustrative dimensions for 2-bit phase shift element **100** were $P=12$ millimeters (mm) for length **120** and width **121**, $l_1=6.5$ mm for arm length **208**, $w_1=1.2$ mm for arm width **206**, $l_2=4.9$ mm for corner arm length **202**, $w_2=2.0$ mm for corner arm width **204**, $s=0.4$ mm for first distance **200**, $h_1=0.81$ mm for third thickness **118**, and $h_2=1.52$ mm for first thickness **116** of first dielectric layer **102**. For illustration, second 2-bit phase shift element **600** can be fabricated using printed circuit board technology. The thickness of the conductive layers may vary based on the laminates used. For example, standard thicknesses for conductive layers of Rogers laminates are 0.017 mm, 0.035 mm, and 0.07 mm. The prototypes fabricated and simulated used copper layers with a thickness of 0.035 mm.

Referring to FIG. **5A**, simulation results for the magnitudes of the reflection coefficients R_{yy} and R_{xx} are shown for Modes 1 and 2 in accordance with the illustrative embodiment. An R_{yy} reflection coefficient curve **500** for Mode 1 and an R_{yy} reflection coefficient curve **502** for Mode 2 are shown relative to the left axis as a function of frequency. An R_{xx} reflection coefficient curve **504** for Mode 1 and an R_{xx} reflection coefficient curve **506** for Mode 2 are shown relative to the right axis as a function of frequency. The polarization rotation behavior in these two modes is shown by a high R_{xx} ($|R_{xx}| > -1$ decibels (dB)) and a low R_{yy} ($|R_{yy}| < -10$ dB) over the frequency range from 9.1 GHz to 11.1 GHz.

Referring to FIG. **5B**, simulation results for the magnitudes of the reflection coefficients R_{yy} and R_{xx} are shown for Modes 3 and 4 in accordance with the illustrative embodiment. An R_{yy} reflection coefficient curve **510** for Mode 3 and an R_{yy} reflection coefficient curve **512** for Mode 4 are shown relative to the left axis as a function of frequency. An R_{xx} reflection coefficient curve **514** for Mode 3 and an R_{xx} reflection coefficient curve **516** for Mode 4 are shown relative to the right axis as a function of frequency. In contrast to the two polarization-rotating modes, R_{yy} is small ($|R_{yy}| < -68$ dB) and R_{xx} is high ($|R_{xx}| > -1$ dB) over the frequency range from 8.0 GHz to 11.0 GHz.

Referring to FIG. **5C**, simulation results are shown for the phases of R_{xy} for Modes 1 and 2 and for the phases of R_{yy} for Modes 3 and 4 in accordance with the illustrative embodiment. An R_{xy} phase curve **520** for Mode 1, an R_{xy} phase curve **522** for Mode 2, an R_{yy} phase curve **524** for Mode 3, and an R_{yy} phase curve **526** for Mode 4 are shown as a function of frequency. Four distinctive phase values, referenced to the phase of R_{xy} of Mode 1, are quite close to 0° , 90° , 180° , and 270° (or -90°) at 10 GHz. The response of 2-bit phase shift element **100** in all four modes is symmetric for x-polarized and y-polarized incident waves meaning $R_{xy}=R_{yx}$ and $R_{xx}=R_{yy}$.

Subsequently, reflection coefficients of 2-bit phase shift element **100** in the four modes were evaluated in simulations for the case where the incident wave is polarized along the u-axis. Referring to FIG. **6A**, simulation results for the magnitudes of the reflection coefficients R_{uu} are shown for Modes 1 through 4 in accordance with the illustrative embodiment. An R_{uu} reflection coefficient curve **600** for Mode 1, an R_{uu} reflection coefficient curve **602** for Mode 2, an R_{uu} reflection coefficient curve **604** for Mode 3, and an R_{uu} reflection coefficient curve **606** are shown as a function of frequency.

Referring to FIG. **6B**, simulation results for the magnitudes of the reflection coefficients R_{vu} are shown for Modes 1 through 4 in accordance with the illustrative embodiment. An R_{vu} reflection coefficient curve **610** for Mode 1, an R_{vu} reflection coefficient curve **612** for Mode 2, an R_{vu} reflection coefficient curve **614** for Mode 3, and an R_{vu} reflection coefficient curve **616** are shown as a function of frequency.

Referring to FIG. **6C**, simulation results for the phases of R_{uu} for Modes 1 through 4 are shown in accordance with the illustrative embodiment where the phase of Mode 1 is taken as the reference. An R_{uu} phase curve **620** for Mode 1, an R_{uu} phase curve **622** for Mode 2, an R_{uu} phase curve **624** for Mode 3, and an R_{uu} phase curve **626** for Mode 4 are shown as a function of frequency. As expected from equations (1) to (4), all four modes provide reflected waves with a dominant polarization along the u-axis. Specifically, the co-polarization reflection coefficient R_{uu} has a magnitude ≥ -1 dB, and the cross-polarization reflection R_{vu} has a magnitude ≤ -57 dB from 9.0 GHz to 11.7 GHz. At 10

GHz, the phase values for the four reflection modes are 0° , 88° , 203° (-157°), and 281° (-79°). Using the phase values of the four modes results in an equivalent bit number of 1.91 bits at 9.5 GHz, 1.94 bits at 10.0 GHz, and 1.92 bits at 10.5 GHz. The equivalent bit number is greater than or equal to 1.7 bits over the frequency range of 9.0-11.5 GHz. The operating frequency range for the 2 bit phase shift element **100** was determined to be from 9.0 GHz to 11.0 GHz, over which the phase resolution is not less than 1.7 bits, and the co-polarization reflection coefficients R_{uu} for all four modes is not less than -1 dB.

Referring to FIG. 7, a 1-D side view of a transceiver system **700** is shown in accordance with an illustrative embodiment. Transceiver system **700** may include a feed antenna **702** and a plurality of 2-bit phase shift elements. Transceiver system **700** may act as a transmitter or a receiver of analog or digital signals. The plurality of 2-bit phase shift elements is arranged to form a reflective array antenna **704**. Feed antenna **702** may have a low gain. Feed antenna **702** may be a dipole antenna, a monopole antenna, a helical antenna, a microstrip antenna, a patch antenna, a fractal antenna, a feed horn, a slot antenna, an end fire antenna, a parabolic antenna, etc. Feed antenna **702** is positioned a focal distance **712**, f_a , from a front face **705** of the plurality of 2-bit phase shift elements. Feed antenna **702** is configured to receive an analog or a digital signal, and in response, to radiate a spherical radio wave **706** toward front face **705** of the plurality of 2-bit phase shift elements. For example, front face **705** may include conducting pattern layer **107** of each 2-bit phase shift element. Feed antenna **702** also may be configured to receive spherical radio wave **706** from front face **705** of the plurality of 2-bit phase shift elements and to generate an analog or a digital signal in response.

The plurality of 2-bit phase shift elements may be arranged to form a one-dimensional (1D) or a two-dimensional (2D) array of spatial phase shift elements in any direction. The plurality of 2-bit phase shift elements may form variously shaped apertures including circular, rectangular, square, elliptical, etc. The plurality of 2-bit phase shift elements can include any number of 2-bit phase shift elements.

Referring to FIG. 8, a perspective view of transceiver system **700** is shown with a circular aperture. Feed antenna **702** is illustrated as a feed horn and is positioned at a center of reflective array antenna **704**. The plurality of 2-bit phase shift elements are arranged to form a circular 2-D array of 2-bit phase shift elements. The plurality of 2-bit phase shift elements has an aperture length **710**.

Spherical radio wave **706** reaches different portions of front face **705** at different times. The plurality of 2-bit phase shift elements can be considered to be a plurality of pixels each of which act as a 2-bit phase shift unit by providing a selected phase shift within the frequency band of interest. Thus, each 2-bit phase shift element of the plurality of 2-bit phase shift elements acts as a phase shift circuit selected such that spherical radio wave **706** is re-radiated in the form of a planar wave **708** that is parallel to front face **705**, or vice versa. Given aperture length **710** and focal distance **712**, the phase shift profile provided for the plurality of 2-bit phase shift elements to form planar wave **708** directed to a specific angle can be calculated as understood by a person of skill in the art. Center **134** of each 2-bit phase shift element is separated a distance **714** from center **134** of its neighbors in any direction. Distance **714** may be equal to length **120** and width **121**.

For example, assuming feed antenna **702** is aligned to emit spherical radio wave **706** at the focal point of the

plurality of 2-bit phase shift elements, the time it takes for each ray to arrive at front face **705** is determined by a length of each ray trace, i.e., the distance traveled by the electromagnetic wave traveling at the speed of light. A minimum time corresponds to a propagation time of the shortest ray trace, which is the line path from feed antenna **702** to a center of front face **705** for a center positioned feed antenna **702**. A maximum time corresponds to a propagation time of the longest ray trace, which is the line path from feed antenna **702** to an edge of front face **705** for the center positioned feed antenna **702**. Feed antenna **702** may be positioned at an off-center position with a resulting change in the distribution of ray traces to each 2-bit phase shift element. Of course, because the distance varies between feed antenna **702** and each 2-bit phase shift element of reflective array antenna **704**, a magnitude of the portion of spherical radio wave **706** received by each 2-bit phase shift element also varies.

Referring to FIG. 9A, a top perspective view of a fabricated reflective array antenna **900** having a circular aperture is shown in accordance with an illustrative embodiment. Referring to FIG. 9B, a bottom perspective view of fabricated reflective array antenna **900** is shown in accordance with an illustrative embodiment to illustrate a distribution pattern of the switch position of the 2-bit phase shift elements of FIG. 9A arranged on bottom surface **400** of first dielectric layer **102** to achieve a beam collimation in the broadside direction. Fabricated reflective array antenna **900** includes 484 2-bit phase shift elements distributed to form a circular 2-D aperture. A second reflective array antenna (not shown) was also fabricated to achieve a beam collimation in 45° relative to the broadside direction.

Each prototype was implemented on three Rogers RO4003C substrates. First dielectric layer **102** had a thickness of 1.52 mm. Second dielectric layer **106** was formed of two layers each having a thickness of 0.81 mm that were bonded together by two layers of 0.1 mm-thick Rogers RO4450F prepregs. The top and bottom metallic layers of each 2-bit phase shift element **100** were connected with plated via holes with diameters of 0.46 mm. The static ON/OFF states of the switches **306**, **307**, **308**, **308** that configured the operating state of each 2-bit phase shift element **100** were implemented by the presence/absence of copper traces with widths of 0.3 mm on the bottom metallic layer. Conducting layer **107** of both fabricated reflective array antenna were identical while the metallic patterns on bottom surface **400** were different according to the switch configurations for realizing beam collimation at 0° and 45° relative to the broadside direction.

Referring to FIG. 10, a top perspective view of the distribution pattern of the switch position of fabricated reflective array antenna **900** is shown to illustrate a bit configuration (reflection mode) of each 2-bit phase shift element across a face of fabricated reflective array antenna **900** having an aperture length **710** of 30 centimeters (cm) to achieve the beam collimation in the broadside direction. A first incident wave vector k_i points in a direction of incident wave propagation from feed antenna **702** positioned at a center of fabricated reflective array antenna **900** with focal distance **712** of 254 mm. A first reflected wave vector k_r points in a direction of reflected wave propagation. Feed antenna **702** was a horn antenna with aperture dimensions of 4×4 cm².

The horn antenna was oriented so that the polarization of the incident wave was along the u-axis, or parallel to a diagonal line of the square shaped unit cells in fabricated reflective array antenna **900**. The horn antenna was simu-

lated and the amplitude and phase distribution of the radiated electromagnetic field in the plane of the intended position of the reflective array was extracted. The phase of the incident electric field at the center of each unit cell $\Phi_{inc}(x_i, y_i)$ and the desired outgoing phase $\Phi_d(x_i, y_i)$ were used to calculate the reflection phase shift that the unit cell needed to provide $\Phi_{ref}(x_i, y_i) = \Phi_d(x_i, y_i) - \Phi_{inc}(x_i, y_i)$.

The desired outgoing phase $\Phi_d(x_i, y_i)$ can be calculated from the direction of the main beam ($\theta_0 = \alpha$ (azimuth) and $\phi_0 = \beta$ (elevation)) in a spherical coordinate system and the coordinate (x_i, y_i) of center **134** of 2-bit phase shift element **100** using

$$\Phi_d(x_i, y_i) = \sqrt{x_i^2 + y_i^2} \sin(\alpha) \cos\left(\tan^{-1}\left(\frac{y_i}{x_i}\right) - \beta\right).$$

Subsequently, the necessary reflection phase shifts of the unit cells, wrapped into the range from -180° to 180° , are quantized into four levels and the operating mode of the unit cells are determined according to the following expression:

$$\text{Mode} = \begin{cases} 1, & \text{if } -45^\circ \leq \Phi_{ref}(x_i, y_i) < 45^\circ \\ 2, & \text{if } 135^\circ \leq \Phi_{ref}(x_i, y_i) \text{ or } \Phi_{ref}(x_i, y_i) < -135^\circ \\ 3, & \text{if } 45^\circ \leq \Phi_{ref}(x_i, y_i) < 135^\circ \\ 4, & \text{if } -135^\circ \leq \Phi_{ref}(x_i, y_i) < -45^\circ \end{cases}$$

Using this method, distribution patterns for the switch positions of the 2-bit phase shift elements on the aperture of reflective array antenna **700** to generate a beam steered to scan angles at 0° , 15° , 30° , 45° , 60° relative to a boresight axis are shown in FIGS. **11A** to **11E**, respectively, in accordance with an illustrative embodiment, where “bit **00**” indicates the first switch positions (first mode) for 2-bit phase shift element **100**, “bit **11**” indicates the second switch positions (second mode) for 2-bit phase shift element **100**, “bit **01**” indicates the third switch positions (third mode) for 2-bit phase shift element **100**, and “bit **10**” indicates the fourth switch positions (fourth mode) for 2-bit phase shift element **100**, where each pixel represents a distinct 2-bit phase shift element **100**.

Referring to FIG. **11A**, a top view of a 0° distribution pattern **1100** of the switch position of reflective array antenna **704** is shown to illustrate a bit configuration (reflection mode) of each 2-bit phase shift element across the face of reflective array antenna **704** to achieve the beam collimation in the broadside direction at 10 GHz. Reflective array antenna **900** was fabricated to have 0° distribution pattern **1100**. Referring to FIG. **11B**, a top view of a 15° distribution pattern **1102** of the switch position of reflective array antenna **704** is shown to illustrate a bit configuration (reflection mode) of each 2-bit phase shift element across the face of reflective array antenna **704** to achieve beam collimation 15° off of the broadside direction at 10 GHz. Referring to FIG. **11C**, a top view of a 30° distribution pattern **1104** of the switch position of reflective array antenna **704** is shown to illustrate a bit configuration (reflection mode) of each 2-bit phase shift element across the face of reflective array antenna **704** to achieve beam collimation 30° off of the broadside direction at 10 GHz. Referring to FIG. **11D**, a top view of a 45° distribution pattern **1106** of the switch position of reflective array antenna **704** is shown to illustrate a bit configuration (reflection mode) of each 2-bit phase shift element across the face of reflective array antenna **704** to

achieve beam collimation 45° off of the broadside direction at 10 GHz. The second reflective array was fabricated to have 45° distribution pattern **1106**. Referring to FIG. **11E**, a top view of a 60° distribution pattern **1108** of the switch position of reflective array antenna **704** is shown to illustrate a bit configuration (reflection mode) of each 2-bit phase shift element across the face of reflective array antenna **704** to achieve beam collimation 60° off of the broadside direction at 10 GHz.

Full-wave simulations of the reflective array antenna **704** were performed for each of the distribution patterns configured for each scan angle 0° , 15° , 30° , 45° , 60° relative to the boresight axis in CST Microwave Studio to evaluate the beam steering performance within the operating frequency range of the unit cell from 9 GHz to 11 GHz.

Referring to FIG. **12A**, a simulated realized gain for the five different beam configurations as a function of zenith angle at 9 gigahertz (GHz) is shown in accordance with an illustrative embodiment. A first 9 GHz gain curve **1200** shows the simulated realized gain for the scan angle 0° at 9 GHz, a second 9 GHz gain curve **1202** shows the simulated realized gain for the scan angle 15° at 9 GHz, a third 9 GHz gain curve **1204** shows the simulated realized gain for the scan angle 30° at 9 GHz, a fourth 9 GHz gain curve **1206** shows the simulated realized gain for the scan angle 45° at 9 GHz, and a fifth 9 GHz gain curve **1208** shows the simulated realized gain for the scan angle 60° at 9 GHz.

Referring to FIG. **12B**, a simulated realized gain for the five different beam configurations as a function of zenith angle at 9.5 GHz is shown in accordance with an illustrative embodiment. A first 9.5 GHz gain curve **1210** shows the simulated realized gain for the scan angle 0° at 9.5 GHz, a second 9.5 GHz gain curve **1212** shows the simulated realized gain for the scan angle 15° at 9.5 GHz, a third 9.5 GHz gain curve **1214** shows the simulated realized gain for the scan angle 30° at 9.5 GHz, a fourth 9.5 GHz gain curve **1216** shows the simulated realized gain for the scan angle 45° at 9.5 GHz, and a fifth 9.5 GHz gain curve **1218** shows the simulated realized gain for the scan angle 60° at 9.5 GHz.

Referring to FIG. **12C**, a simulated realized gain for the five different beam configurations as a function of zenith angle at 10 GHz is shown in accordance with an illustrative embodiment. A first 10 GHz gain curve **1220** shows the simulated realized gain for the scan angle 0° at 10 GHz, a second 10 GHz gain curve **1222** shows the simulated realized gain for the scan angle 15° at 10 GHz, a third 10 GHz gain curve **1224** shows the simulated realized gain for the scan angle 30° at 10 GHz, a fourth 10 GHz gain curve **1226** shows the simulated realized gain for the scan angle 45° at 10 GHz, and a fifth 10 GHz gain curve **1228** shows the simulated realized gain for the scan angle 60° at 10 GHz.

Referring to FIG. **12D**, a simulated realized gain for the five different beam configurations as a function of zenith angle at 10.5 GHz is shown in accordance with an illustrative embodiment. A first 10.5 GHz gain curve **1230** shows the simulated realized gain for the scan angle 0° at 10.5 GHz, a second 10.5 GHz gain curve **1232** shows the simulated realized gain for the scan angle 15° at 10.5 GHz, a third 10.5 GHz gain curve **1234** shows the simulated realized gain for the scan angle 30° at 10.5 GHz, a fourth 10.5 GHz gain curve **1236** shows the simulated realized gain for the scan angle 45° at 10.5 GHz, and a fifth 10.5 GHz gain curve **1238** shows the simulated realized gain for the scan angle 60° at 10.5 GHz.

Referring to FIG. **12E**, a simulated realized gain for the five different beam configurations as a function of zenith

angle at 11 GHz is shown in accordance with an illustrative embodiment. A first 11 GHz gain curve **1240** shows the simulated realized gain for the scan angle 0° at 11 GHz, a second 11 GHz gain curve **1242** shows the simulated realized gain for the scan angle 15° at 11 GHz, a third 11 GHz gain curve **1244** shows the simulated realized gain for the scan angle 30° at 11 GHz, a fourth 11 GHz gain curve **1246** shows the simulated realized gain for the scan angle 45° at 11 GHz, and a fifth 11 GHz gain curve **1248** shows the simulated realized gain for the scan angle 60° at 11 GHz.

For the same scan angle, the beam shapes are consistent and the gain variation is within 1.3 dB across the different frequency points. At 10 GHz, the peak realized gain is 26.2 dBi for $\theta_0=0^\circ$, 26.2 dBi for $\theta_0=15^\circ$, 25.4 dBi for $\theta_0=30^\circ$, 24.2 dBi for $\theta_0=45^\circ$, and 22.4 dBi for $\theta_0=60^\circ$. The scan loss for steering the beam from broadside to a scan angle of 45° is about 1.2 dB at 9.0 GHz, 1.7 dB at 9.5 GHz, 2 dB at 10 GHz, 2.4 dB at 10.5 GHz, and 1.7 dB at 11.0 GHz. For a scan angle up to 60° , the scan loss is about 2.8-3.8 dB within the 9-11 GHz frequency range. The maximum gain variation within the scan angle range of $\pm 45^\circ$ and over the entire operating frequency range is about 3 dB. Moreover, side lobe levels are less than -13.3 dB for all scan angles at all five frequency points.

A static 2-bit and a static 1-bit reflective array antenna **704** were simulated to assess the improvement of using 2-bit phase shift element **100** over a 1-bit phase quantization. Both simulated reflective array antennas had the same aperture dimensions and were fed by the same antenna with the same focal distance. The 1-bit reflective array antenna **704** was populated by 1-bit phase shifters having the two polarization rotating modes similar to Modes 1 and 2 of 2-bit phase shift element **100**. The phase shifters on both arrays were configured following corresponding 1-bit and 2-bit Fresnel patterns for beam collimation at the broadside direction at 10 GHz.

Referring to FIG. **13**, a comparison between a simulated radiation pattern computed for the 2-bit reflective array antenna **704** and for the 1-bit reflective array antenna **704** as a function of zenith angle at 10 GHz is shown in accordance with an illustrative embodiment. The 2-bit reflective array antenna **704** as shown by a first curve **1300** provides a maximum realized gain of 26.2 dBi which is 3.5 dB higher than a maximum realized gain of 22.7 dBi provided by the 1-bit reflective array antenna **704** as shown by a second curve **1304**. Additionally, the 2-bit reflective array antenna **704** exhibits a 7-dB lower side lobe level compared to the 1-bit reflective array antenna **704**. Moreover, the maximum, normalized cross-polarization level of the 2-bit reflective array antenna **704** as shown by a third curve **1302** is about 8 dB lower than that of the 1-bit reflective array antenna **704** as shown by a fourth curve **1306**. Of course, the improvement in the peak gains, side lobe levels, and polarization purity of using the 2-bit phase shifters comes at the expense of reduced bandwidths.

Referring to FIG. **14**, a comparison between a simulated peak gain computed for the 2-bit reflective array antenna **704** as shown by a fifth curve **1400** and for the 1-bit reflective array antenna **704** as shown by a sixth curve **1402** as a function of frequency is shown in accordance with an illustrative embodiment. The 3-dB gain bandwidths are from 8.9 GHz to 11.2 GHz (23%) for the 2-bit reflective array antenna **704** and from 8.6 GHz to 11.6 GHz (30%) for the 1-bit reflective array antenna **704**. Therefore, for applications that do not require bandwidths of larger than 23%, 2-bit phase shift element **100** can be used to provide significant

improvement in beam collimation performance of reflective array antennas compared to 1-bit phase shifters.

Radiation patterns were characterized for both of the fabricated antennas using a near-field spherical measurement system placed inside an anechoic chamber. During the measurements, a styrofoam fixture was used to position feed antenna **702** at the desired focal distance and to align its E-plane properly with respect to the reflective array antennas fabricated.

Referring to FIG. **15A**, a comparison between the simulated and the measured radiation patterns as a function of angle at 10 GHz in the E-plane for a main beam centered at 0° is shown in accordance with an illustrative embodiment. Referring to FIG. **15B**, a comparison between the simulated and the measured radiation patterns as a function of angle at 10 GHz in the H-plane for a main beam centered at 0° is shown in accordance with an illustrative embodiment. The measured radiation patterns were generated using reflective array antenna **900**. The measured realized gain at the broadside direction of reflective array antenna **900** was 26.5 dBi as shown by a seventh curve **1500** for the E-plane and as shown by an eighth curve **1510** for the H-plane, which agrees well with the predicted value of 26.2 dBi in the full-wave simulations as shown by a ninth curve **1502** for the E-plane and as shown by a tenth curve **1512** for the H-plane. Reflective array antenna **900** provided side lobe levels lower than -18.5 dB in both cut planes while the simulated side lobe levels were less than -19.5 dB in the E-plane and -18.1 dB in the H-plane. The measured cross-polarization levels, normalized to the maximum realized gain, were below -22.9 dB in the E-plane and -26.2 dB in the H-plane. These cross-polarization levels are slightly higher than the simulated values which were less than -23.2 dB and -30.3 dB in the E-plane and H-plane, respectively.

Referring to FIG. **16**, a comparison between the simulated and the measured radiation patterns as a function of angle at 10 GHz in the H-plane for a main beam steered to 45° relative to the boresight axis is shown in accordance with an illustrative embodiment. The measured radiation patterns were generated using the second reflective array antenna that was fabricated with 45° distribution pattern **1106** shown referring to FIG. **11D**. The peak measured gain of the co-polarization pattern was 23.8 dBi at $\theta_0=45^\circ$ as shown by an eleventh curve **1600**, which is about 0.4 dB smaller than the predicted value in the full-wave simulations as shown by a twelfth curve **1602**. The measured side lobe levels of less than -18.9 dB was slightly lower than the simulated values of less than -18.1 dB. A more pronounced difference between the measurement and simulation results was observed in the cross-polarization levels in the direction of the main beam. Specifically, the second reflective array antenna provided a significantly higher polarization purity of 22.5 dB as shown by a thirteenth curve **1604** compared to the simulated value of 14.1 dB as shown by a fourteenth curve **1606**. The discrepancies between the measurement and simulation results of the two prototypes can be partly attributed to fabrication tolerances, uncertainties in measurements, and the dielectric properties of the Rogers materials used for constructing the second reflective array antenna, as well as slight errors in positioning and aligning feed antenna **702** with respect to the second reflective array antenna. Other components of the measurement setup that were not taken into account in the full wave simulations such as the styrofoam fixture, a short section of coaxial-to-waveguide transition used for feed antenna **702**, and a coaxial cable connecting feed antenna **702** to a test port of the measurement chamber also contributed to these discrepancies. Nev-

ertheless, the measurement and simulation results show reasonable agreement in terms of key features such as directions of the main beam, peak gains, and side lobe levels for both fabricated reflective array antennas.

As used herein, the term “mount” includes join, unite, connect, couple, associate, insert, hang, hold, affix, attach, fasten, bind, paste, secure, bolt, screw, rivet, solder, weld, glue, form over, form in, layer, mold, rest on, rest against, etch, abut, and other like terms. The phrases “mounted on”, “mounted to”, and equivalent phrases indicate any interior or exterior portion of the element referenced. These phrases also encompass direct mounting (in which the referenced elements are in direct contact) and indirect mounting (in which the referenced elements are not in direct contact, but are connected through an intermediate element). Elements referenced as mounted to each other herein may further be integrally formed together, for example, using a molding or a thermoforming process as understood by a person of skill in the art. As a result, elements described herein as being mounted to each other need not be discrete structural elements. The elements may be mounted permanently, removably, or releasably unless specified otherwise.

The word “illustrative” is used herein to mean serving as an example, instance, or illustration. Any aspect or design described herein as “illustrative” is not necessarily to be construed as preferred or advantageous over other aspects or designs. Further, for the purposes of this disclosure and unless otherwise specified, “a” or “an” means “one or more”. Still further, using “and” or “or” in the detailed description is intended to include “and/or” unless specifically indicated otherwise. The illustrative embodiments may be implemented as a method, apparatus, or article of manufacture using standard programming and/or engineering techniques to produce software, firmware, hardware, or any combination thereof to control a computer to implement the disclosed embodiments.

Any directional references used herein, such as left-side, right-side, top, bottom, back, front, up, down, above, below, etc., are for illustration only based on the orientation in the drawings selected to describe the illustrative embodiments.

The foregoing description of illustrative embodiments of the disclosed subject matter has been presented for purposes of illustration and of description. It is not intended to be exhaustive or to limit the disclosed subject matter to the precise form disclosed, and modifications and variations are possible in light of the above teachings or may be acquired from practice of the disclosed subject matter. The embodiments were chosen and described in order to explain the principles of the disclosed subject matter and as practical applications of the disclosed subject matter to enable one skilled in the art to utilize the disclosed subject matter in various embodiments and with various modifications as suited to the particular use contemplated.

What is claimed is:

1. A phase shift element comprising:

a first dielectric layer including a top, first dielectric surface and a bottom, first dielectric surface, wherein the top, first dielectric surface is on an opposite side of the first dielectric layer relative to the bottom, first dielectric surface, wherein the first dielectric layer is formed of a first dielectric material;

a conductive layer including a top conductive surface and a bottom conductive surface, wherein the top conductive surface is on an opposite side of the conductive layer relative to the bottom conductive surface, wherein the bottom conductive surface is mounted to the top,

first dielectric surface, wherein the conductive layer is formed of a first conductive material;

a second dielectric layer including a top, second dielectric surface and a bottom, second dielectric surface, wherein the top, second dielectric surface is on an opposite side of the second dielectric layer relative to the bottom, second dielectric surface, wherein the bottom, second dielectric surface is mounted to the top conductive surface, wherein the second dielectric layer is formed of a second dielectric material;

a conducting pattern layer including a plurality of conductors mounted to the top, second dielectric surface, wherein the conducting pattern layer is formed of a second conductive material, wherein each conductor of the plurality of conductors is orthogonal to two other conductors of the plurality of conductors;

a plurality of switches mounted to the bottom, first dielectric surface, wherein each switch of the plurality of switches is configured to be switchable between a conducting position and a non-conducting position; and

a plurality of vertical interconnect accesses (vias), wherein each vertical interconnect access (via) of the plurality of vias is formed of a third conductive material that extends through the first dielectric layer, through a third dielectric material formed in and through the conductive layer, and through the second dielectric layer, wherein each via of the plurality of vias is connected to a single conductor of the plurality of conductors;

wherein the first conductive material is configured to reflect an electromagnetic wave incident on the conducting pattern layer and on the second dielectric layer, wherein, when a switch of the plurality of switches is in the conducting position, the switch electrically connects two conductors of the plurality of conductors to each other through their respective vias,

wherein a plurality of different switch configurations of the plurality of switches provide a 2-bit phase quantization on the reflected electromagnetic wave relative to the electromagnetic wave incident on the conducting pattern layer when the electromagnetic wave is incident on the conducting pattern layer.

2. The phase shift element of claim 1, wherein at least one of the first conductive material, the second conductive material, and the third conductive material is a different conductive material.

3. The phase shift element of claim 1, wherein at least one of the first dielectric material, the second dielectric material, and the third dielectric material is a different dielectric material.

4. The phase shift element of claim 1, wherein the first dielectric layer is formed of a plurality of layers of different dielectric materials.

5. The phase shift element of claim 1, wherein the first dielectric material is air.

6. The phase shift element of claim 1, wherein a number of the plurality of conductors is four and a number of the vias is four.

7. The phase shift element of claim 6, wherein each switch of the plurality of switches is a single pole, single throw switch, and a number of the plurality of switches is four.

8. The phase shift element of claim 1, wherein a first switch of the plurality of switches is configured to electrically connect a first via to a second via, wherein a second switch of the plurality of switches is configured to electrically connect the second via to a third via, wherein a third switch of the plurality of switches is configured to the third

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via to a fourth via, and wherein a fourth switch of the plurality of switches is configured to electrically connect the fourth via to the first via.

9. The phase shift element of claim 8, wherein each conductor of the plurality of conductors has an arrow shape comprised of a first arrow tip arm, a second arrow tip arm, and a shaft.

10. The phase shift element of claim 9, wherein the first arrow tip arm is perpendicular to the second arrow tip arm.

11. The phase shift element of claim 9, wherein the shaft of each arrow shape is rotated by 90 degrees relative to an adjacent shaft.

12. The phase shift element of claim 9, wherein the shaft of each arrow shape is pointed outward from a center of the plurality of conductors.

13. The phase shift element of claim 9, wherein the shaft electrically connects the first arrow tip arm and the second arrow tip arm to a respective via of the plurality of vias.

14. The phase shift element of claim 13, wherein a first switch configuration includes the first switch electrically connecting the first via to the second via, the second switch electrically connecting the second via to the third via, the third switch in the non-conducting position, and the fourth switch in the non-conducting position.

15. The phase shift element of claim 14, wherein a second switch configuration includes the first switch electrically connecting the first via to the second via, the fourth switch electrically connecting the fourth via to the first via, the second switch in the non-conducting position, and the third switch in the non-conducting position.

16. The phase shift element of claim 15, wherein a third switch configuration includes the first switch electrically connecting the first via to the second via, the second switch electrically connecting the second via to the third via, the third switch electrically connecting the third via to the fourth via, and the fourth switch electrically connecting the fourth via to the first via.

17. The phase shift element of claim 16, wherein a fourth switch configuration includes the first switch, the second switch, the third switch, and the fourth switch in the non-conducting position.

18. The phase shift element of claim 1, wherein a first electrical path length of each conductor of the plurality of conductors in combination with the respective via is approximately a quarter of a wavelength $\lambda_0/4$, where $\lambda_0=c/f_0$, where c is a speed of light, and f_0 is a central operating frequency of the incident electromagnetic wave.

19. The phase shift element of claim 18, wherein a second electrical path length of each switch in the conducting position is less than $\lambda_0/5$.

20. A phased array antenna comprising:

a first dielectric layer including a top, first dielectric surface and a bottom, first dielectric surface, wherein the top, first dielectric surface is on an opposite side of the first dielectric layer relative to the bottom, first dielectric surface, wherein the first dielectric layer is formed of a first dielectric material;

a conductive layer including a top conductive surface and a bottom conductive surface, wherein the top conduc-

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tive surface is on an opposite side of the conductive layer relative to the bottom conductive surface, wherein the bottom conductive surface is mounted to the top, first dielectric surface, wherein the conductive layer is formed of a first conductive material;

a second dielectric layer including a top, second dielectric surface and a bottom, second dielectric surface, wherein the top, second dielectric surface is on an opposite side of the second dielectric layer relative to the bottom, second dielectric surface, wherein the bottom, second dielectric surface is mounted to the top conductive surface, wherein the second dielectric layer is formed of a second dielectric material; and

a plurality of phase shift elements distributed in a direction, wherein each phase shift element of the plurality of phase shift elements comprises

a conducting pattern layer including a plurality of conductors mounted to the top, second dielectric surface, wherein the conducting pattern layer is formed of a second conductive material, wherein each conductor of the plurality of conductors is orthogonal to two other conductors of the plurality of conductors;

a plurality of switches mounted to the bottom, first dielectric surface, wherein each switch of the plurality of switches is configured to be switchable between a conducting position and a non-conducting position; and

a plurality of vertical interconnect accesses (vias), wherein each vertical interconnect access (via) of the plurality of vias is formed of a third conductive material that extends through the first dielectric layer, through a third dielectric material formed in and through the conductive layer, and through the second dielectric layer, wherein each via of the plurality of vias is connected to a single conductor of the plurality of conductors;

wherein the first conductive material is configured to reflect an electromagnetic wave incident on the conducting pattern layer and on the second dielectric layer, wherein, when a switch of the plurality of switches is in the conducting position, the switch electrically connects two conductors of the plurality of conductors to each other through their respective vias,

wherein a plurality of different switch configurations of the plurality of switches provide a 2-bit phase quantization on the reflected electromagnetic wave relative to the electromagnetic wave incident on the conducting pattern layer when the electromagnetic wave is incident on the conducting pattern layer,

wherein a switch configuration of each phase shift element of the plurality of phase shift elements is selected such that the plurality of phase shift elements generates a main beam of the reflected electromagnetic wave in a preselected direction when the electromagnetic wave is incident on the conducting pattern layer.

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